Perception of Surrounding Sound Source Trajectories in the Horizontal Plane: A Comparison of VBAP and Basic-Decoded HOA

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Summary

Despite the fundamental role played by sound in multiple virtual reality contexts, few studies have explored the perception of virtual sound source motion in the acoustic space. The goal of this study was to compare the localization of virtual moving sound sources rendered with two different spatialization techniques: Vector Base Amplitude Panning (VBAP) and fifth-order Ambisonics (HOA), both implemented in a soundproofed room and in their most basic form (basic decoding of HOA, VBAP without spread parameter). The perception of virtual sound trajectories surrounding untrained subjects ($n=23$) was evaluated using a new method based on a drawing-augmented multiple-choice questionnaire. In the spherical loudspeaker array used in this study, VBAP proved to be a robust spatialization technique for sound trajectory rendering in terms of trajectory recognition and height perception. In basic-decoded HOA, subjects exhibited far more disparate trajectory recognition and height perception performances but performed better in perceiving sound source movement homogeneity.

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1. Introduction

Virtual reality is increasingly used in ever more applications, from leisure pursuits (e.g. video games) to industrial contexts (from assembly method prototyping [1]) to education and medicine (e.g. psychotherapy [2]). Sound plays a fundamental role in virtual reality through its capacity to convey information and to reinforce the experience of immersion [3]. Yet sound display has long been neglected compared with video. Numerous techniques can, however, create immersion through sound, using headphones [4] or loudspeakers to spatialize the sound sources [5]. These systems, known as Virtual Auditory Displays (VADs), allow the synthesis of a virtual acoustic space, creating virtual sources that can be moved freely in the acoustic space. Virtual moving sound sources delivered by VAD are already used in various research and musical applications. Thus, the question of the perceptual rendering of these sound source movements is fundamental.

These techniques are not always implemented in an anechoic environment (e.g. in a concert hall, or a reality apparatus such as CAVE), and the room hosting the VAD often impacts the sound field produced [6]. We are interested here in the perceptive rendering of moving sources in what we call an “actual implementation”: a normal room

whose sound reflections are not perfectly compensated. Since a virtual moving sound source can be reproduced by means of different techniques, it is pertinent to determine which technique is the most reliable for moving sound reproduction. In this paper, we choose to focus on moving sound perception in a VAD, comparing two fundamentally different spatialization techniques, both implemented in a normal room: High Order Ambisonics (HOA) and Vector Based Amplitude Panning (VBAP).

The HOA approach aims at reconstructing a 3D sound field using a loudspeaker array [7]. The sound field is first projected on a spherical harmonics basis, which gives an intermediate spatial description of it [8]. Then, the plane-wave-based approximation of this 3D sound field can be reconstructed at one particular point, after a decoding step taking into account the surrounding loudspeaker system [9]. By contrast, VBAP is an extension of stereophony to 3D, which simulates the position of sound sources using perceptual illusions. VBAP distributes the signal onto two or three loudspeakers according to a panning law to create phantom sources (a source which is perceived in-between loudspeakers). Although some authors consider VBAP and HOA as respectively related to a perceptual and a physical approach [10], we will here refer to global vs local panning. The HOA approach (global panning) uses the whole loudspeaker array to reconstruct the sound field, whereas with VBAP (local panning), only a subset of loudspeakers is used.

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In the present study, we compare VBAP and HOA in terms of perception of sound source trajectories surrounding the subjects. This issue of perception of sound trajectories was raised by a previous study in which we addressed the influence of a rotating auditory stimulus on the postural regulation of standing subjects [11]. In that study, the postural sway of subjects was measured while they were exposed to various rotating stimuli. The rotating sound sources were traveling along a virtual circle surrounding the subjects at ear level, and rendered using third-order HOA. At the end of the experiment, the subjects were informally questioned about their perception of sound trajectories. Trajectory perception appeared to vary widely among subjects. Moreover, the trajectories reported by the subjects were often quite different from the trajectories presented (for example, an arc of a circle, or a straight line instead of a circle). This variability could have been introduced by the sound spatialization method used in this experiment, which is why we consider it vital to determine the impact of the sound reproduction approach on dynamic auditory localization performances.

2. Background: perception of moving sound sources

There have been few investigations into localization of moving sound sources in the acoustic space. Yet, perception of moving sound has been extensively studied through a wide variety of paradigms (see Carlile and Leung [12] for a global overview of the topic).

Most studies on moving sound perception focused on determining different kinds of motion perception thresholds. They usually investigated the Minimum Auditory Moving Angle (MAMA), defined as the smallest angle a sound must travel before its direction is correctly discriminated. Extensive work in this field was originally carried out by Grantham [13] and Perrott [14], and investigations on MAMA continued thereafter (see for example a recent paper by Lewald [15]). These studies helped to characterize auditory motion perception resolution, showing for example that this resolution decreases (greater MAMA) when sound source velocity increases, or is poorer in the vertical plane than in the horizontal plane. Other studies focused on velocity perception: the velocity discrimination threshold [16] or the weight of acoustic cues used in velocity perception [17]. Similarly, Lufti and Wang investigated the weight of different acoustic cues in the discrimination of sound source displacement, velocity and acceleration [18]. More generally, the motion perception threshold was addressed via other paradigms. A study conducted by Feron *et al.* [19] investigated the upper limits of auditory motion perception by determining the point at which a sound rotating around the listener is no longer resolvable as such. They found that beyond a speed of 3 rotations per second, subjects are no longer able to hear a rotating sound. In another study by Yost *et al.* [20], subjects were asked whether or not they perceived sound source motion in various conditions in which the listeners (eyes open or

closed) and/or the source were rotated. As variations in acoustic cues used for sound localization can be caused either by source motion or self-motion, this study aimed at investigating which additional sensory cues the listener uses to identify the cause of the variations in acoustic cues.

In addition, some studies explored the motion extrapolation of auditory trajectories, through “predicting motion” tasks. In these experiments, listeners are presented with a looming sound source (i.e., an approaching sound stimulus) that stops playing on the way; they are then asked to judge when the source would have reached them if it had continued to move toward them at the same speed [21]. While the first studies were unimodal (with auditory stimuli), later studies involved bimodal stimuli (auditory-visual targets) to determine the weight of each input in the motion extrapolation [22, 23].

Other research directions explored perceptual illusions induced by sound source displacement: auditory motion after-effect (a bias in static sound source localization that occurs after repeated presentation of a moving sound source [24]), or auditorily-induced illusory self-motion (also calledvection - see Valjamae [25] for a review).

There have been only a few brief investigations of perception of the trajectories themselves, rarely leading to publications. The earliest contribution we found in the literature is an informal test conducted by Blauert [26] (page 272), in which a rotating trajectory on a 6-loudspeaker ring in the azimuthal plane was simulated around the listener, using amplitude and phase modulations of a sinusoidal signal. According to the delay of the phase modulation, Blauert reported the perception of either an ellipse at a positive elevation or the intended circular trajectory. Then, in a study conducted in a Virtual Auditory Display using VBAP, authors investigated the perception of various trajectories in the frontal plane. They showed that changes in azimuth were better perceived than changes in elevation, which were perceived stepwise, and that measured trajectories had a tendency to bend towards the loudspeaker positions [27]. In another study comparing binaural rendering and VBAP rendering with 8 or 24 loudspeakers, the authors synthesized a complex trajectory that “seemed like a fly moving in and out all around the listener” [28]. The study was only conducted on 4 subjects, and the methods and results analysis lack clarity; however, their results suggest that a larger configuration of speakers can support a more accurate perception of complex auditory motion. Another study conducted by Dunai *et al.* [29] using binaural rendering of impulse train sounds addressed the influence of the inter-click interval on sound localization accuracy. Trajectories were pseudo-random variable distance displacements rendered in the frontal plane. The authors demonstrated that the best localization results were achieved for an inter-click interval of 150 ms; moreover, better localization accuracy was obtained in azimuth than in distance. Another study conducted by Caro Moreno [30] compared the localization and the sound coloration of circle and square trajectories, spatialized using VBAP on different loudspeaker rings (14, 28 or 56 loudspeaker-

ers). Their results showed that increasing the number of loudspeakers improved the trajectory localization but induced a detrimental sound coloration. Finally, Marentakis and McAdams also investigated trajectory perception on a VAD but pursuing a different goal: the perceptual impact of gesture control of spatialization [31]. Their experiment compared trajectory recognition by subjects exposed to 1 - a unimodal condition (auditory stimulus alone rendered in VBAP) and 2 - a bimodal condition in which a “performer” made gestures congruent or incongruent with the sound trajectory. The congruent gestures were found to enhance trajectory recognition whereas incongruent gestures impeded it, as the listener’s attention was shifted to incongruent visual cues.

This review of the literature on moving sound perception shows that the few studies addressing trajectory recognition used VBAP or binaural techniques, but none used HOA. Moreover, to date these different techniques have not been directly compared. To fill this gap, we systematically address the issue of the perception of sound source trajectories rendered by Virtual Auditory Displays (VAD) using both VBAP and HOA techniques. As a preamble to this study, we decided to compare the precision of static sound source localization in VBAP and HOA. We found that VBAP was more precise than HOA, especially in elevation perception and in front-back confusion rate [32]. In the present paper, our objective is to determine whether these trends persist when moving sound sources are used.

3. Methods

Our study investigated the perception of sound source trajectories in the horizontal plane, using two different sound spatialization systems: Vector Base Amplitude Panning (VBAP) and High Order Ambisonics (HOA). This required sound trajectories to be rendered with a 3D sound spatialization system and a new response interface to be designed.

3.1. Subjects

The study group consisted of 23 subjects (9 women and 14 men) aged between 20 and 59 (mean±std: 30.4±9.5 years). Subjects were students or researchers from acoustics or microbiology laboratories. A few subjects had previous experience in psychoacoustic experiments but none of them could be considered experts in sound localization. None of the subjects reported auditory loss. All of them participated on a volunteer basis and signed an informed consent form prior to testing. This study was performed in accordance with the ethical standards of the Declaration of Helsinki (revised Edinburgh, 2000).

3.2. Experimental set-up: spherical loudspeaker array

The experimental set-up consisted of a sound spatialization system making it possible to immerse subjects in an acoustic field. Forty-two loudspeakers were equally

Figure 1. The spherical loudspeaker array.

Table I. Loudspeaker positions in spherical coordinates (azimuth and elevation) in degrees. Coordinates in bold stand for the subset of 18 loudspeakers used to simulate horizontal trajectories in VBAP (in HOA, the 42 loudspeakers were active).

az	el	az	el	az	el	az	el
-60	-69	158	-35	-150	0	98	35
60	-69	0	-21	150	0	-142	35
180	-69	-120	-21	0	11	142	35
0	-53	120	-21	-120	11	-60	53
-120	-53	60	-11	120	11	60	53
120	-53	-60	-11	-60	21	180	53
-38	-35	180	-11	60	21	0	69
38	-35	-30	0	180	21	-120	69
-82	-35	30	0	-22	35	120	69
82	-35	-90	0	22	35		
-158	-35	90	0	-98	35		

distributed on the vertices of a metallic geodesic sphere (see Figure 1). A geodesic sphere is a discretized sphere formed by a complex network of triangles. Here, the F2 frequency geodesic sphere contained 42 vertices and 120 bars. The bars were simply screwed onto the junctions and separated by rubber slivers to limit the transmission of vibrations. Thus the loudspeakers screwed onto the junctions were acoustically de-coupled from the metal structure. The diameter of the metal structure was 3m20, meaning that the 42 loudspeakers were positioned on an imaginary sphere approximately 3 meters in diameter. This distance is sufficient for the loudspeakers to be considered to deliver plane waves. The precise position of the loudspeakers on the sphere is given in Table I. The angular gap between two adjacent loudspeakers was either 31.7° or 36°. Due to the nature of the spatialization techniques compared in this study, the two algorithms did not use the same number of loudspeakers: in VBAP, only the 18 loudspeakers closest to the azimuthal plane were excited (see

Table I), whereas in HOA, all the 42 loudspeakers were active.

The loudspeakers were Genelec 8020C two-channel active monitoring systems (frequency response: 65 Hz – 21 kHz). The room hosting the structure measured approximately 5 x 4 x 4 m and was not perfectly rectangular. Effective soundproofing was provided by rockwool lining the walls and carpet on the floor, so that the reverberation time was between $RT_{60} = 538$ ms at $f = 125$ Hz and $RT_{60} = 155$ ms at $f = 8000$ Hz (further details in the Appendix). The overall background noise level was 24 dB_A.

The subjects were positioned inside the loudspeaker structure, with their heads in the very center of the sphere.

A fuller description of the system as well as the results of a static sound source localization test conducted in the system can be found in [32].

3.3. Stimuli

As stated in the introduction, this work is motivated by the results of a previous study in which we addressed the influence of a rotating auditory stimulus on the postural regulation of standing subjects [11]. In that study, where we used a pink noise sound source rotating at various speeds on a circular trajectory centered on the subject, perception of sound trajectories was observed to vary widely among subjects. Here, the sound stimuli (sound source nature, speed and trajectories) were chosen principally so as to reproduce the sound stimulation used in that previous study.

Thus, the dynamic sound source was a pink noise rotating at an angular speed of 180°/s (the speed which had resulted in the strongest postural effects in our previous study), far below the upper limits of auditory rotational motion perception [19]. This source traveled along five different trajectories around the subject: three circles (centered on the subject, shifted 0.5 m forward, shifted 0.5 m to the right), and two ellipses (front-back or left-right direction)(see Figure 2). The radius of the circle trajectories was set at $r = 2$ m, in accordance with the size of the spatialization system: the radius of the system was 1.5 m, and ambisonic synthesis without NFC¹ does not allow sound sources to be positioned inside the sphere of loudspeakers. Therefore for circles with a 2 m radius, the sound source was traveling outside the sphere, both when centered and when shifted. For the ellipse trajectories, we set the semi-major axis at $a = 3$ m and the semi-minor axis at $b = 1.5$ m. Thus, the eccentricity e was $e = \sqrt{a^2 + b^2}/a = 0.86$, which is close to 0.9, a value known to match the perceptive prototypical ellipse geometry [34].

All these trajectories were set on the horizontal plane at ear level. Both the direction of the rotation (clockwise or anti-clockwise) and the beginning of the trajectory were chosen randomly.

The trajectories were rendered using two different spatialization techniques: VBAP and HOA (at fifth order). Sound spatialization was produced using Ircam

Figure 2. Top view of the five trajectories presented to the subjects in the experiment (trajectories were randomized in direction).

SPAT software (www.forum.ircam.com) in a Max/MSP (www.cycling74.com) environment². Each spatialization technique was used in its most basic form. For HOA, *basic* decoding was used, no optimization such as *maxRe* or *inPhase* was applied, and encoding was done without NFC³. Similarly, for VBAP, the *spread* parameter of the multiple-direction VBAP algorithm was not used. These processes of technique optimization and hybridization will be further discussed in the discussion section.

At the center of the system, where the listener was positioned, the sound amplitude was 50.5 dB_A in VBAP and 54 dB_A in HOA for the centered circular trajectory (for the other trajectories it was not possible to measure sound amplitudes, as the distance between the source and the center kept varying). Rather than setting the same sound amplitude for both spatialization techniques, we equalized it relative to the perceived loudness. HOA involves more channels than VBAP, thereby producing higher amplitudes of sound for the same loudness.

For both spatialization techniques, two sound source morphology features were used to better simulate displacement. First, SPAT integrated sound amplitude diminishing with distance from the listener (“drop” parameter set at 6, meaning that the energy of the source is reduced by 6 dB each time the distance doubles [35]). Then, we added a Doppler effect producing changes in the sound amplitude and the frequency content of the sound source (this latter effect did not modify the source dramatically). These tools, especially amplitude variation [36], make it possible to simulate variation in distance, which is included in neither VBAP nor HOA (as implemented here, without NFC) theory. However, we chose the size of the trajectories, i.e. the radii of the circles and ellipses, such that the distance between the listener and the sound source did not vary substantially, which prevented the content of the sound from being affected by sharp morphological changes [37]. It should be noted that the aim of this study was not to examine how the morphological attributes of sound impact the perception of sound source displacement, but rather to explore the precision of the spatial reproduction achieved using HOA and VBAP techniques.

3.4. User response interface

This experiment required us to develop a specific interface for the subjects to report their responses. In static

¹ The Near Field Compensation developed by Daniel [33].

² More details on the Max/MSP settings are given in the Appendix.

³ More details on the HOA parameters are given in the Appendix.

sound localization studies, pointing (hand or head pointing [38], eye pointing, etc.) is generally used to report subjects' answers. However pointing tasks are difficult to adapt to dynamic studies, especially if the trajectories are not rendered solely in the frontal plane, as in our experiment. Some static localization studies also used the God's Eye Localization Pointing (GELP) technique, a technique in which the subjects indicate the perceived direction of the sound by pointing at a scale model sphere [39]. This could be adapted to dynamic localization, by asking the subjects to draw the perceived trajectory around a scale model sphere representing their head. However the technique is known to induce a significant bias due to the representation of space [40], and subjects training would be required to ensure reliable results.

The few dynamic sound localization studies we mentioned in the introduction used either a Multiple-Choice Questionnaire (MCQ) allowing the subjects to choose between various fixed trajectories [31], or free 2D drawing of the trajectories [29, 28]. While MCQ results are easy to analyze, this method may be too restrictive and may influence subject choices. On the other hand, drawings can be complex to post-treat and may raise tricky questions like how to compare an ellipse and a more complex shape such as an eight loop.

We therefore decided to implement a new method combining MCQ and 2D drawings to obtain an "augmented MCQ". A graphical user interface was designed in Max/MSP and included various questions together with a drawing option. This interface was then put on a tablet using FantaStick (pinktwins.com/fantastick), an application enabling communication via WiFi between Max/MSP and a tablet in front of the subject (cf Figure 3). For each trial, the subject had to answer questions concerning the perceived trajectory. The questions (below) ranged from the more general, to avoid influencing their judgment, to the more detailed depending on their previous answers:

- Did you perceive the trajectory around you, in front of you or behind you?
- Which kind of trajectory did you perceive? Here, the choice offered depended on the previous answer: "circle" or "ellipse" if the subject's previous answer was "around"; "straight line" or "arc of a circle" if their previous answer was "behind" or "in front".
- On the basis of the first two answers, the described trajectory was graphically represented on the user interface. Subjects were then given the opportunity to intuitively shift (with one finger) or rotate (with two fingers) the represented trajectory so as to position it according to their perception.
- At this stage, if subjects were not satisfied with the screen representation, they were given the option of freely drawing the trajectory.
- Finally, the subjects had to evaluate three attributes of the perceived trajectory, moving a slider (without unit feedback):

Figure 3. Configuration of the experiment inside the spherical loudspeaker array.

- the perceived height of the trajectory (set at 0 by default for listener head height; minimum and maximum were set at sphere diameter ± 1.5 m),
- the inclination of the trajectory plane (set at 0 by default; minimum and maximum were set at $\pm 90^\circ$),
- the fluidity of the sound source displacement, described to subjects as the smoothness and the homogeneity of the displacement they perceived.

An overview of the interface through 4 screenshots is given in Figure 4. This new interface allowed subjects to report quickly and precisely the trajectory they heard. It also has the advantage of providing various levels of answer: general answers that are easy to process (e.g. surrounding trajectory or not) and more detailed answers (e.g. drawings).

3.5. Procedure

Subjects stood with their head placed at the center of the rendering system and maintained in a fixed position with a chinstrap (see Figure 3). The height of the platform was adjusted to allow for the different heights of the subjects. They were asked to close their eyes during the presentation of the sound trajectory and were told to trigger the stimulus themselves when they felt ready.

The sound trajectory was presented for 15 seconds (7.5 rotations around the listener); then, subjects could follow the procedure on the interface as described in the previous section, submit their response and trigger the next stimulus. Response time was not limited.

The only information that the subjects were given about the nature of the trajectories they were listening to was that the sound source was moving on a plane. Subjects were not informed that all the trajectories were surrounding them and moving on the horizontal plane alone. Subjects were not trained in sound localization or on the user interface usage before starting the experiment.

The experiment contained a total of 50 stimuli: 2 spatialization techniques $\times$ 5 trajectories $\times$ 5 repetitions. The order of presentation of stimuli and spatialization techniques was randomized into 5 blocks of 10 trials. The

Figure 4. Screen shots of the graphical user interface displayed on the tablet.

whole experiment lasted between 30 and 45 minutes, depending on subject speed.

3.6. Data analysis

We first analyzed the data from the drawings, fitting an ellipse automatically on each drawing using a least-square criterion method. Each fit was then checked: if the fit matched the trajectory drawn, the drawing was replaced by this ellipse in individual subjects' data. If not, the drawing was kept unmodified and the answer was considered as "other".

The user response interface designed for this experiment made it possible to obtain different levels of response. Some responses were categorical: place where the trajectory was perceived (around, in front, behind) and the type of trajectory perceived (circle, ellipse, arc of a circle, straight line, other). Others yielded continuous parameters, such as perceived height, fluidity, inclination and position of the center of the trajectory.

First, the "surrounding" nature of the trajectory was analyzed, to investigate whether it was perceived to be surrounding or not. A binomial set of data (1 if the trajectory was perceived to surround subjects/ 0 if not) was analyzed here using a mixed effects logistic regression.

Then, the relevant continuous parameters were analyzed via a linear mixed effects analysis followed by a Tukey's post hoc test.

All the statistical analyses were conducted using R [41] with lme4 package [42]. For all the results presented in

the next section, visual inspection of residual plots did not reveal any obvious deviations from homoscedasticity or normality. P-values were obtained by likelihood ratio tests testing the full model with the effect in question against the model without the effect in question. Then, planned comparisons were performed when necessary.

4. Results

Given that the response interface was custom designed for this experiment and previously untried, the subjects were questioned informally at the end of the experiment about their experience with the interface. Overall, they were satisfied with the interface (for most of the trials, they were able to report the trajectory they perceived and its characteristics without difficulty).

To avoid any possible confusion between the use of "trajectory" to mean the trajectory presented to the subjects (sound stimulus) and the trajectory they perceived (subject response), we chose in the following to label the former "stimulus trajectory" and the latter "response trajectory".

4.1. Categorical parameters: recognition of the trajectories

The categorical parameters were analyzed using a mixed effect logistic regression. As fixed effects, the spatialization technique, the stimulus trajectory and the repetition were entered into the model. As random effects, there were intercepts for subjects.

1. Surrounding nature of the trajectory and inter-subject variability

The perception percentage for each trajectory according to spatialization technique and stimulus trajectory is presented in Figure 5. With the VBAP technique, subjects were much more likely to report surrounding trajectories (more than 90% circles and ellipses reported for each trajectory type) than with the HOA technique (around 60% on average). This difference was found to be significant ($\chi^2(1) = 273.67, p < 0.0001$). No significant effect on the perception percentage of surrounding trajectories was revealed for stimulus trajectory, nor any interaction between stimulus trajectory and spatialization techniques. Here, it should be noted that sound trajectory recognition was highly subject-dependent, as shown in Figure 6. Some subjects were able to hear circles and ellipses in most cases, whereas others reported numerous straight lines, arcs of a circle or even more complex shapes. Moreover, this variability was not equal for the two spatialization techniques. Figure 6 shows that the variability was mainly in HOA perception, with the rate of perception of surrounding trajectories varying between 0 and 100%. By contrast, with VBAP the rate of perception of surrounding trajectories varied only between 80 and 100%.

To better characterize this variability, the individual distribution of subjects' answers was further observed. Figure 7 illustrates the disparity between subjects, with 6 different subjects exhibiting various performance levels in

Figure 5. Distribution of subjects' responses as a function of stimulus trajectory and spatialization technique.

Figure 6. Percentage of surrounding trajectories reported by each subject, depending on the spatialization technique. The red dots and circles are for the subjects whose response distribution is represented in Figure 7. Variability is very high in HOA (between 0 and 100%) and low in VBAP (between 80 and 100%).

HOA recognition. The two upper plots are for subjects achieving a good recognition of surrounding trajectories in both spatialization techniques (subjects 6 and 21); the two middle plots represent the results for subjects achieving medium-level recognition of surrounding trajectories rendered in HOA (subjects 12 and 14); the lower plots are for subjects achieving poor recognition of surrounding trajectories in HOA (subjects 9 and 22).

These plots also show that not all subjects were consistent in their responses. For example, whereas subject 6 gave really consistent responses and reported mainly ellipses even in the circle stimulus conditions, subject 9 re-

Figure 7. Examples of individual distributions of responses as a function of stimulus trajectory and spatialization technique, for 6 different subjects. Recognition of the surrounding nature of the trajectory was good for all subjects in VBAP, but highly variable in HOA. Top: two subjects with good surrounding trajectory recognition under both techniques (100% surrounding trajectory recognition in HOA too). Middle: two subjects with a **medium-level** trajectory recognition rate in HOA. Bottom: two subjects with a **poor** trajectory recognition rate in HOA.

ported varying proportion of circles and ellipses in all the conditions.

2. Types of trajectories

Figure 5 shows that circles and ellipses were frequently confused, especially for the circle trajectories. Confusions occurred with both spatialization techniques. Centered circle: VBAP yielded 35% reports of ellipses against 60% of circles, while HOA yielded 15% reports of ellipses against 40% of circles. Shifted circles: VBAP yielded around 50% reports of ellipses against 40% of circles, HOA around 30% reports of ellipses against 30% of circles. Ellipses: there were around 10% reports of circles with both spatialization techniques, and reports of ellipses came to 90% for VBAP and 50-60% for HOA. Figure 7 shows that the rate of confusion between circles and ellipses is subject-dependent, but not correlated with recognition that the tra-

jectories were surrounding the subject. For instance Subject 9, whose surrounding trajectory recognition was poor (0% in HOA), had a low rate of confusion between circles and ellipses in VBAP. Conversely, Subject 6 reported 100% of surrounding trajectories in HOA and VBAP, but frequently confused circles and ellipses under both spatialization techniques.

4.2. Continuous parameters: trajectory characteristics

The continuous parameters were analyzed using a mixed effect linear regression. As fixed effects, the spatialization technique and the stimulus trajectory were entered into the model. As random effects, there were intercepts for subjects. Here, the repetition factor was not entered into the model, as the effect of repetition was of no interest and because the continuous parameters could be averaged over the various repetitions, unlike the categorical parameters.

1. Perceived height of the trajectory

The results for perceived height of the trajectory are presented in Figure 8. They clearly show that the trajectories were perceived to be higher under the HOA technique (0.5 meters high on average) than when using VBAP (around 0 meters high). This result is significant ($\chi^2(1) = 185.41, p < 0.0001$). No significant effect of stimulus trajectory and no interaction between spatialization technique and stimulus trajectory were found.

2. Fluidity of the sound source displacement

Results for perceived fluidity of the sound source displacement are presented in Figure 8. We can see that the trajectories were perceived to be more homogeneous under the HOA technique when using VBAP. This result is significant ($\chi^2(1) = 46.23, p < 0.0001$). No significant effect of stimulus trajectory and no interaction between spatialization technique and stimulus trajectory were found.

3. Inclination of the trajectory

No significant effect of spatialization technique or stimulus trajectory was found on the inclination of the trajectory: the inclination was around zero degrees on average.

4. Center of the trajectory

Results for the position of the center of the perceived trajectory, showing whether the subjects were able to perceive the shift in the circle, are reported in Figure 9. The linear regression highlighted a significant effect of stimulus trajectory on the position of the center of the trajectory in both directions (front-back: $\chi^2(4) = 40.32, p < 0.0001$, left-right: $\chi^2(4) = 45.20, p < 0.0001$). For the front-back direction, the Tukey post-hoc test showed that for the second stimulus (circle shifted forward), subjects reported one trajectory whose center was positioned significantly differently from that of the other four trajectories ($p < 0.001$). For the left-right direction, the Tukey post-hoc test showed that for the third stimulus (circle shifted to the right), subjects reported one trajectory whose center was positioned significantly differently from that of the

Figure 8. Left: Boxplot representing the perceived height of the trajectory for the two spatialization techniques. Right: Boxplot representing the perceived fluidity (arbitrary unit) of the sound source displacement trajectory for the two spatialization techniques. Red dots represent the mean.

Figure 9. Boxplot representing the position of the center of the trajectory (arbitrary unit) perceived by subjects as a function of the five stimulus trajectories. Red dots represent the mean. Left: Position along the antero-posterior axis (front-back). Right: Position along the medio-lateral axis (left-right).

other four ($p < 0.01$). There was no effect of the spatialization technique and no interaction between the spatialization technique and the stimulus trajectory. These results show that the subjects were able to perceive the shift of the circle with both spatialization techniques.

5. Discussion

This experiment aimed at comparing the perception of surrounding sound source trajectories rendered using two different sound spatialization techniques: Vector Base Amplitude Panning (VBAP) versus fifth-order Ambisonics with basic decoding (HOA). The experiment was conducted on untrained subjects of various ages without reported hearing loss. All the stimulus trajectories presented to the subjects used pink noise traveling on a circle or an ellipse around the subjects (five different trajectories), on the horizontal plane at ear level. Thanks to a specially designed graphical user interface, subjects could report their perceptions of the different trajectories (choosing from cir-

cles, ellipses, straight lines, arcs of a circle or free drawings).

In the results section, we showed that trajectory recognition varied widely among subjects, mainly when HOA was used. We will first discuss the general results for the whole group and then the inter-subject variability.

5.1. General results

The main differences found between VBAP and HOA concerned 1- the degree to which subjects felt surrounded by the trajectories, 2- the height and 3- the fluidity of the trajectories.

5.1.1. Subjects felt more surrounded by the VBAP trajectories

Firstly, subjects exhibited a significantly higher trajectory recognition rate with VBAP than with HOA. The first descriptor investigated here was the surrounding nature of the trajectory. Subjects reported surrounding trajectories far more with VBAP (around 90-95%) than with HOA (around 60%), for which they reported a lot of arcs of a circle or straight lines. Even though the subjects were not trained in sound spatialization and localization tasks, the VBAP technique here allowed more robust reproduction of sound trajectories. This is in line with results previously obtained with static sources [32].

This difference between perceptions in HOA and VBAP could be explained by the nature of these techniques. VBAP distributes the input signal over various loudspeakers, which distorts Interaural Level Differences (ILD). However it does not impact either low frequency Interaural Time Differences (ITD) or high frequency spectral cues, which remain valid [43]. Subjects localizing a virtual source rendered in VBAP can therefore rely on these auditory cues. Conversely, HOA recreates an approximation of a 3D sound field using an intermediate spatial representation of the sound field. This spatial description is truncated at a point depending on the order of the HOA system. The truncation limits the reconstruction of the sound field; it induces a cutoff frequency in the HOA system, which depends on the area of reconstruction and the order of the system [44]. At fifth order, and for an area including an average head, the cutoff frequency is about 3000 Hz. Above this cutoff frequency, the sound field reconstruction is degraded.

Moreover, HOA reconstructs a perfect sound field up to 3000 Hz only where there is no obstruction. However, the listener's head positioned within the area of reconstruction, causes a frequency-dependent obstruction of the loudspeaker contributions, thereby distorting the sound field. Thus, all the acoustic cues are degraded, including the high-frequency spectral cues known to allow the listener to resolve ambiguities in sound source localization [26]. The deterioration of the spectral cues may induce confusions (e.g., front-back confusions which are known to be frequent in untrained subjects [45] and when the subject's head is fixed). These potential confusions could explain the fact that some subjects perceived arcs of a circle

or even straight lines instead of the circles and ellipses presented to them.

The difference between VBAP and HOA may also be explained by the room effect. VBAP is a local panning method, using only 3 loudspeakers simultaneously, whereas HOA is a global panning method activating the 42 loudspeakers at the same time. With local panning, the sound field produced in the listening room may be less sensitive to the room effect than with global panning. The room effect is crucial when attempting to reproduce precise sound fields with multichannel sound reproduction systems; several techniques have been developed to compensate for it (see for example the active room compensation [6]).

A closer precise investigation of the trajectory perception here shows that subjects had difficulty discriminating between circles and ellipses, whatever the sound spatialization technique. The confusion rate between circles and ellipses was uniformly high, especially for the three circle stimuli (between 30–50% confusion for both spatialization techniques). This result is probably due to the fact that distance cues were voluntarily not fully implemented (see section 2.3), but were simulated mainly through varying the source intensity. We did not provide fundamental distance cues such as direct-to-reverberant energy ratio (we used no reverberation) or filtering due to air absorption. This may have prevented subjects from reliably assessing source distance variation [36], and thus from discriminating between circles and ellipses, especially since they were not familiar with the sound source.

It should be noted, however, that our aim here was to compare the precision of sound trajectory synthesis obtained with different spatialization techniques, not to investigate the absolute human ability to perceive sound trajectories. The confusions between circles and ellipses observed with both spatialization techniques could be due either to the subjects' limited perception skills, or to artifacts in trajectory reproduction related to the sound spatialization techniques. The next step in this research could be to produce a sound source physically rotating around subjects and evaluate its perception with the same user interface. Then we could compare the results of both experiments and assess separately 1) the human ability to perceive sound trajectories and 2) the ability of sound spatialization techniques (and systems) to reliably synthesize sound trajectories.

5.1.2. Trajectories are perceived too high in HOA

Concerning perception of height, the elevation of the trajectory was better perceived in VBAP than in HOA: on average, trajectories in VBAP were perceived at ear level, while in ambisonics they were generally perceived too high. An obvious explanation for this tendency is the way sound source trajectories are rendered in ambisonics. In HOA, the 42 loudspeakers of our system always had to be active to reconstruct the 3D sound field. However, our ambisonic system was calibrated without any subject inside. The presence of a subject inside the sphere undoubtedly

caused absorption of the downward loudspeaker contribution, thereby deforming the sound field rendered by the system and resulting in distorted monoral cues. This sound field distortion may explain the differences in height perception, although further experiments will be required for confirmation.

5.1.3. HOA: more fluidity of displacements

In contrast, the HOA technique scored higher than VBAP on the fluidity of the sound source displacement. When the sound source approaches one loudspeaker, VBAP is known to perceptually provoke a ‘magnetization’ of the sound source on this loudspeaker, i.e. the virtual source is perceived as closer to the loudspeaker than it should be [46]. Here, we chose to investigate trajectory fluidity because with VBAP we were expecting a magnetization effect on loudspeakers close to the horizontal plane. This magnetization should cause the trajectory to be perceived as less smooth and more disturbed, which appears to be borne out here.

5.1.4. Hybridization of spatialization techniques

On the whole, the HOA technique was found here to be less efficient than VBAP in reproducing dynamic trajectories with precision, causing the subjects to report many more wrong trajectories, and to perceive the trajectories too high. However, VBAP suffers from poor fluidity and homogeneity of the sound source displacement. To overcome the mutual limitations of these techniques, other techniques and optimizations have been developed as compromises between local and global panning approaches. For example, HOA decoding has been optimized for better perceptual results: *maxRe* optimization of HOA maximizes the energetic contributions of the loudspeakers closest to the virtual sound source [47], whereas *inPhase* optimization deletes the contributions of the loudspeakers opposite the sound sources [48]. These optimizations were first designed to better cope with imperfect set-up situations (i.e. when the listener is not placed at the center of the system). *maxRe* optimization has been shown to improve static localization performances as compared to basic decoding in HOA [49]. More recently, another HOA decoding technique directly based on VBAP panning techniques was developed [50]. Zotter *et al.* [51] also developed a reverse hybridization of VBAP and HOA, with VBAP-based HOA decoding, designed for irregular loudspeaker arrangements. Thus, despite of the scarcity of studies addressing perceptual differences between spatialization techniques, these HOA optimizations suggest a growing awareness that better perceptual results are obtained using local panning approaches such as VBAP. The present study offers quantitative results to support this view. They highlight the gap between the approximations of a soundfield reproduced with basic-decoded HOA, based on an ideal scenario, and the reality of human perception.

There is also evidence that VBAP’s limitations that can be overcome using principles inspired from the ambisonic approach. For example, Pulkki [52] implemented

a multiple-direction VBAP algorithm to better control the spread of a sound source and avoid changes in spread when the source is moved (when a virtual signal seems to come from the direction of a loudspeaker, the virtual source is consistently localized on this loudspeaker, whereas when it is panned between loudspeakers, it appears spread). This approach uses more loudspeakers than the original triplet to better control sound source spreading and to limit magnetization of the source on the loudspeaker, thereby obtaining a more faithful rendering than original VBAP. A similar approach by Borss [53] uses N-wise panning with polygons instead of triplets of loudspeakers.

5.2. High variability in HOA perception

The difference in trajectory recognition between VBAP and HOA varied widely among subjects. At first glance, this high inter-subject variability in response to the two techniques is surprising. However, it can be explained by the unusual nature of the task (tracking a sound source and imagining its trajectory), the subjects’ lack of familiarity with the stimulus (pink noise is an abstract source), the fact that subjects had their head fixed and, above all, the fact that subjects were not trained in sound spatialization perception. Closer investigation of individual responses showed, however, that this variability mainly stems from subjects’ widely differing HOA perception: subjects had a uniformly good trajectory recognition rate in VBAP. This observation confirms that the variability did not come from the response interface. All the subjects were satisfactorily enabled to report their perceptions, a confirmation reinforced by informal feedback from the subjects after the test. Moreover, it proves that the variability of the results is not due to some subjects’ hearing problems.

Some subjects’ trajectory recognition performances were good under both sound spatialization techniques. They reported only a few non-surrounding trajectories and showed few differences in performance between spatialization techniques (see the upper plots of Figure 7). Other subjects exhibited huge differences between techniques, reporting in HOA many (or solely) arcs of a circle and straight lines (see the bottom plots of Figure 7). Some subjects fell between these two extremes, with medium-level performances in HOA (middle plots in Figure 7). Numerous subjects thus seemed to have difficulties using the complex signals produced in HOA to accurately perceive the displacement of a sound source along its trajectory. These subjects may have been more sensitive to the errors of approximation inherent in the HOA rendering, resulting in biased spatial perception of the trajectories rendered in HOA. It would be interesting to determine, using a larger subject sample, if these results reflect a continuum of perceptual judgments, or whether the subjects can be grouped according to their ability to perceive sound spatialized in HOA.

The causes of such variability in perception of the auditory environment are also worth exploring. At the beginning of the experiment, we collected some information on each subject: sex, age, left- or right-handedness,

and expertise in music and sound perception (the latter via two closed-ended questions: “Are you a musician?” and “Are you used to auditory perception tests?”). None of these factors was able to predict the subjects’ performances in HOA perception, with the two extremes - i.e. good and poor recognition of surrounding trajectories - containing both young and old subjects, musicians and non-musicians, men and women, etc.

A parallel can be drawn with stereoscopic visualization on digital displays. Stereoscopy is a visual illusion of depth created by means of two images showing different views of a scene. A proportion of the population has difficulty properly combining the horizontal binocular disparities of the two images and perceiving depth: they are said to be “stereoblind”. Stereoblindness has been consistently reported to affect 14% of the population [54]. Optometric vision training allows stereopsis recovery [55]. Similarly, in spatial audio perception, some people seem to have more difficulty perceiving complex 3D sound fields generated in ambisonics. Perhaps training, already known to improve static localization performances [56], could help them achieve better results.

6. Conclusion

To our knowledge, this study is the first to compare the perception of VBAP and HOA methods in a Virtual Auditory Display using surrounding trajectories. Overall, in our system and under our protocol conditions (basic decoding of HOA, untrained subjects), VBAP provided better scores on trajectory recognition and height perception, whereas HOA provided better scores on sound source displacement fluidity. With both techniques, subjects had difficulties discriminating between circles and ellipses, suggesting either insufficient precision in the reproduction of trajectory and distance cues or the inadequate perceptual skills of untrained subjects.

Moreover, a high inter-subject variability clearly emerged from our results: whereas some subjects’ trajectory recognition performances were good in both spatialization techniques, others were good in VBAP but poor in HOA. The reason for this variability remains an open question and an exciting challenge for the auditory perception field.

This study’s finding highlight the importance of choosing the sound spatialization technique to be used in a virtual reality context according to the sound scenario intended. Recent theoretical developments of methods hybridizing local and global panning techniques to overcome their mutual limitations are promising, although the perceptual evaluation of such technologies requires further investigation.

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Table II. Mean reverberation time in the experimental room as a function of the frequency.

F (Hz)	TR (s)
125	0.538
250	0.205
500	0.228
1000	0.244
2000	0.208
4000	0.191
8000	0.155

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Appendix

Reverberation Time

For a room hosting a multichannel sound reproduction system, BS.1116 standard recommends a mean reverberation time of $T_m=230 \text{ ms} \pm 0.05 \text{ s}$ between 200 Hz and 4000 Hz; $T_m=230 \text{ ms} \pm 0.01 \text{ s}$ between 4000 Hz and 8000 Hz. The mean reverberation times measured in the various octave bands are presented in Table II.

Max/MSP characteristics

Sampling Frequency: 48000 Hz

Signal Vector Size: 512

I/O Vector Size: 512

A new panning position was calculated every 10.7 ms.

HOA Decoding parameters

Order: 5

Decoding method: energy preserving [10]

Decoding type: basic

Decoding norm: SN3D

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