Weathering-limited hillslope evolution in carbonate landscapes

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Abstract

Understanding topographic evolution requires integrating elementary processes acting at the hillslope scale into the long-wavelength framework of landscape dynamics. Recent progress has been made in the quantification of denudation of eroding landscapes and its links with topography. Despite these advances, data is still sparse in carbonate terrain, which covers a significant part of the Earth’s surface. In this study, we measured both long-term denudation rates using in situ-produced \textsuperscript{36}Cl concentrations in bedrock and regolith clasts and surface convexity at 12 sites along ridges of the Luberon carbonate range in Provence, Southeastern France. Starting from \textasciitilde30 mm/ka for the lowering of the summit plateau surface, denudation linearly increases with increasing hilltop convexity up to \textasciitilde70 mm/ka, as predicted by diffusive mass transport theory. Beyond this point denudation rates appear to be insensitive to the increase in hilltop convexity. We interpret this constant denudation as indicating a transition from a regime where hillslope evolution is primarily controlled by diffusive downslope regolith transport, toward a situation in which denudation is limited by the rate at which physical and chemical weathering processes can produce clasts and lower the hilltop. Such an abrupt transition into a weathering-limited dynamics may prevent hillslope
denudation from balancing the rate of base level fall imposed by the river network and could potentially explain the development of high local relief in many Mediterranean carbonate landscapes.

Keywords Landscape evolution; Carbonates; Denudation; Cosmogenic nuclides; Hillslope processes

1 Introduction

Our understanding of landscape dynamics relies on the ability to predict rates of denudation from the measurement of topographic properties. The possibility of establishing a causal link between the two has been greatly enhanced over the last two decades, mainly due to several critical methodological breakthroughs. First, the availability of high resolution representations of the topographic surface, through LiDAR or photogrammetric techniques, has allowed the systematic measurement of elevation over length-scales that are relevant for the elementary geomorphic processes at work, in particular across hillslopes [e.g. Roering et al., 1999; Perron et al., 2008]. Second, we can now measure in situ-produced cosmogenic nuclides concentrations in various near-surface materials, allowing accurate quantification of the rates of geomorphic processes. The combination of these spatial and temporal constraints has allowed the investigation and validation of several Geomorphic Transport Laws [Dietrich et al., 2003] pertaining to first-order open questions in landscape evolution [e.g. Small et al., 1999; Roering et al., 2007; Hurst et al., 2012; Johnstone and Hilley, 2015; Foster et al., 2015]. For example, based on a simple conceptual model for the evolution of soil-mantled hillslopes [Gilbert, 1909; Culling, 1960], field observations of diagnostic relationships between landscape morphology (slope angles, curvature) and rates of evolution (downslope regolith transport, denudation) are direct hints of the occurrence of specific processes [e.g. McKean et al., 1993; Heimsath et al., 1997; Anderson, 2002; Hurst et al., 2012].

Many of the aforementioned studies have focused on the evolution of landscapes developed on quartz-rich lithologies, where the measurement of in situ-produced $^{10}$Be concentrations in bedrock or regolith materials provided direct constraints on processes timescales. Recent advances on the calibration of $^{36}$Cl production rate from Ca spallation have opened the way for the implementation of similar approaches in carbonate landscapes [Stone et al., 1994; Schimmel, 2009]. For example, Ryb et al. [2013, 2014b,a] have provided important insights into the spatial distribution of denudation for carbonate dominated landscapes across a strong climatic gradient in Israel.
The significant control of the precipitation gradient on the denudation pattern support the idea that dissolution is the major regulator of the evolution of such landscapes and that physical processes play only a secondary role, unless water availability becomes limiting for chemical weathering. However, in many carbonate landscapes hillslopes display convex hilltops that are commonly associated with diffusion-like regolith transport [Gilbert, 1909; Culling, 1960]. These observations suggest that physical weathering and regolith transport may play a significant role in the evolution of carbonate hillslopes in addition to total dissolution. Due to their frequent occurrence, especially in Peri-Mediterranean regions, it is of major interest to understand the dynamics of carbonates dominated landscapes, in particular to assess to what extent the evolution processes and Geomorphic Transport Laws that have been proposed and validated for soil mantled hillslopes are transferable to these settings.

The purpose of this study is to provide such quantitative insights into the dynamics of these landscapes and hillslopes through the combination of detailed morphological measurements with estimates of denudation based on in situ-produced cosmogenic nuclides inventories. We focused on the carbonate ranges of Provence in South-Eastern France which provide an ideal setting for such investigations. In particular we test if the fundamental relationship between surface curvature and denudation, which is often considered diagnostic of diffusive transport over regolith-mantled hillslopes, holds in these type of environments. We observe a two-stage evolution, with first a linear increase of denudation rates with hilltop curvature, as predicted by linear diffusion transport theory, and then a plateau where denudation is almost constant despite increasing curvature. We interpret this transition as the consequence of a limit in the ability of weathering processes to produce regolith fast enough to match hillslope transport capacity. We postulate that such evolution could lead to the decoupling of hillslopes evolution from the channels incising at their bottom and promote relief growth in carbonate landscapes.

In this paper, we first present the geological and geomorphological settings of the carbonate ranges of Western Provence, and in particular the Luberon massif where our investigation is focused. After presenting the methodology used to determine denudation rates from cosmogenic nuclides ($^{36}$Cl) measurements and hilltop curvature from the production of high resolution Digital Elevation Models, we introduce a simple 1D hillslope evolution model that allows combining the data obtained by both previous methods. At last, after reporting the main data and results we discuss the significance of the observed transition for the mechanisms of landscape evolution in carbonate domains.
2 Setting

The sedimentary sequence of Western Provence is dominated by a thick Mesozoic platform carbonate series that was deformed during Cenozoic orogenesis. This led to the development of narrow ranges with significant relief, which provide an ideal setting to investigate the evolution of carbonate landscapes (figure 1A). We targeted an area of the Western Luberon mountain (Petit Luberon, figure 1B), a 600 m tall, E-trending and 20 km-long range. It consists mostly of lower Cretaceous carbonates, with Urgonian facies reef limestones outcropping along the crest and northern flank of the range. The Luberon mountain was first uplifted during the Late Cretaceous and Early Eocene Pyrenean tectonic regime. Another major tectonic episode occurred between 10 and 6 Ma prior to the Messinian Salinity Crisis, and led to rejuvenation of the relief and incision [Molliex et al., 2011; Clauzon et al., 2011].

Denudation rates on weathering surfaces across south-eastern France ranges from 20 to 60 mm/ka [Siame et al., 2004; Sadier et al., 2012; Molliex et al., 2013]. The lower bound corresponds to tectonically stable areas, whereas higher values are associated with actively uplifting surfaces.

We selected a specific area of the northern flank of the range, where several regularly spaced north-south ridges are connected with a summit surface (figure 1C). Their well-developed convex profiles suggest that slope-dependent transport is likely contributing to hillslope evolution (figure 2A-B). The low curvature summit surface is being progressively dismantled by regressive erosion along the main valleys draining the southern and northern flanks. This transient evolution is also reflected in the morphology of the ridges, which show significant increases in convexity with distance from the summit (figure 1C). Hillslopes become steeper away from the main crest and ultimately develop steep cliff faces associated with narrow gorges in the lower part of the range (figures 1 and 8).

The climate consists of a combination of Mediterranean and continental characteristics. Available records in Bonnieux (Altitude 250 m asl, figure 1B) over the 1981-2010 period indicate mean annual precipitation is 750 mm/yr, mean minimum annual temperature is 8°C (1°C between December and February) and frost is present for 50 days per year. Our sites are located much higher on the crest of the range, between 600 and 700 m asl, and are directly exposed to the dominant wind (North-South blowing Mistral), suggesting that the conditions they experience are likely to be significantly colder. The ridges host sparse Mediterranean vegetation characterized by small shrubs and shallow grass. The surface is covered by thin but dense regolith (<10 cm in most places) consisting of limestone clasts in the 1-10 cm size range and discontinuous shallow sandy to silty soil pockets (10 to 20 cm deep in most places).
The dimension of these clasts make them transportable by biotic and frost wedging processes. Bedrock outcrops are widespread along these ridges and display a dense network of incipient dissolution features that contribute to clast production. This joint occurrence of meter-scale bedrock patches and thin discontinuous regolith is observed both on hilltops and hillslope flanks, with no clear downslope thinning or thickening trend for the regolith layer.

Bedrock and regolith observed along the crests have undergone both chemical weathering and physical disaggregation. Dissolution features are widespread on both bedrock outcrops and regolith clasts (figure 2E-F). Carbonate dissolution contributes to the progressive rounding of rock fragments and to the development and widening of a network of discontinuities in the rock mass (lapiaz) which in many cases produces transportable clasts. There is also widespread evidence of active fracture development (figure 2C), which appears to be related to thermal stresses and frost cracking but is also probably assisted by bioturbation and the development of the root network. We note that the production of clasts is also greatly facilitated by pre-existing tightly spaced fracture planes that are prevalent at most bedrock outcrops (figure 2D).

3 Methods

3.1 Sampling strategy

We focus on a single area within which relationships between denudation and morphology can be isolated under constant climate and lithology. Our sites are located on top of the ridges, where no regolith flux from above is contributing to the hillslope evolution. We use in situ-produced $^{36}$Cl concentrations measured in both bedrock and regolith fragments (1-10 cm size range) to quantify denudation rates at 12 sites. $^{36}$Cl accumulates in near surface carbonates mainly due to nuclear reactions induced by cosmic ray interaction with Calcium. Hilltop curvature was determined using Digital Surface Models derived from pairs of high resolution aerial photographs at the same sites where we obtained estimates for denudation rates.

3.2 Sample preparation and measurements

Chlorine was extracted from our samples according to the standard protocol used in CEREGE [Schlagenhauf et al., 2010]. Bedrock and amalgamated clasts samples were crushed and sieved to extract the 250-1000 µm fraction.
For each sample ∼50 g were loaded in Nalgene bottles and were submitted to three 5-hours cycles of leaching with MQ water and mechanical shaking. Further sample cleaning was done with a HNO₃ (2M) leaching, resulting in the dissolution of ∼10% of the sample mass. The samples were then dried, weighted and spiked with ∼0.3 g of a Cl solution, with a concentration of 6.92±0.05 mg/g and $^{35}$Cl/$^{37}$Cl and $^{36}$Cl/$^{37}$Cl ratios of 917.8±4.4 and 2.72±0.50×10⁻¹², respectively. Total dissolution of the carbonates was performed with HNO₃ (2M). The solution was filtered and the residues weighted. We then added ∼3 ml of an AgNO₃ solution (100 mg/g) for AgCl precipitation (3 days storage in the dark). The precipitate was dissolved in NH₄OH (1:1) and ∼1 ml of Ba(NO₃)₂ solution was added for sulfate precipitation. Filtering allowed to remove the BaSO₄ precipitate, and final AgCl precipitation was achieved by adding ∼2 ml NNO₃ (1:1). The precipitate was dried and stored in the dark until its final loading in targets for AMS measurements.

Measurements of the chlorine isotopic ratios were performed at the French AMS National Facility, ASTER, located at CEREGE in Aix-en-Provence [Merchel et al., 2008; Arnold et al., 2013]. A KNSTD1600 standard was used with assigned ratios for $^{36}$Cl/$^{35}$Cl, $^{36}$Cl/$^{37}$Cl and $^{35}$Cl/$^{37}$Cl of 2.112×10⁻¹², 6.603×10⁻¹² and 3.127, respectively [Sharma et al., 1990; Fifield et al., 1990].

### 3.3 Hilltop curvature measurements

New algorithms in photogrammetry have allowed this technique to emerge as an alternative tool to Lidar in studies requiring very high resolution topography. Advances in computer vision and image analysis have generated innovative developments in photogrammetry through Structure-from-Motion (SfM) technique, which offers an automated method for the production of high-resolution models with standard cameras [e.g. James and Robson, 2012; Westoby et al., 2012]. This is achieved with calibrated cameras knowing the extrinsic orientation parameters. The identification of tie points between image pairs is done automatically and efficiently using the Scale Invariant Feature Transform (SIFT) algorithm, and the results are optimized and converted in an absolute reference frame using ground control points known precisely in a geodetic system. Then the transform from image to object geometry is performed by bundle rays block adjustment. It consists in a cost optimization function for the 3D structure and the viewing parameters. The outputs of the methods are primarily a dense 3D point cloud, and one can produce also a Digital Surface Model and an orthophotography by projecting the point cloud on a defined plane.

We used aerial photographs acquired by the Institut Géographique National
(IGN), that were processed with Agisoft Photoscan Professional software suite to generate a high density point cloud. The sparse vegetation of this area allows a bare-Earth terrain model to be created, with only limited clipping of isolated bushes required. The point cloud was registered in RGF93, resulting in a typical density of 2.7±1.1 points/m².

Calculations were performed on the point cloud in circular neighbourhoods centred around the sampling sites along the ridges. The size of this neighbourhood is based on the transition between the short wavelength signal associated with surface roughness and vegetation to the long wavelength signal of ridge and valley topography [Roering et al., 2010; Hurst et al., 2012], and in our case was set to 15 m (figure 4). Changing this radius in the 10-30 m range or performing the calculation on the gridded Digital Elevation Model rather than on the point cloud slightly modified the values of the computed curvatures, but did not affect the general first-order trend in the dataset.

We follow the approach of Hurst et al. [2012, 2013b] by fitting a quadratic surface to the neighbourhood around our sampling site,

\[ z(x, y) = ax^2 + by^2 + cxy + dx + ey + f \]  

And curvature \( C \) can be expressed from the coefficients of equation 1 as,

\[ C = 2a + 2b \]  

### 3.4 Hillslope evolution model

We develop a simple hillslope evolution model to understand the relations between denudation and curvature in this landscape. Geomorphic Transport Law (GTL)-based models of hillslope evolution have been extensively applied to the investigation of the behaviour of soil mantled landscapes in most situation underlain by silicate rich substrata [e.g. Anderson, 2002; Dietrich et al., 2003; Roering et al., 2004; Mudd and Furbish, 2004; Roering, 2008; Yoo et al., 2009; Pelletier and Perron, 2012; Pelletier et al., 2013]. We are well aware that carbonate landscapes have, in comparison, received far less attention, and that the formulation of some processes are not yet completely validated in such environments. With these limitations in mind, our purpose is not to perform an extensive parameter space exploration, but rather to test the implications of simple assumptions for processes operating at the scale of the hillslope.

Our model is based on a simple statement of conservation for the regolith cover (thickness \( h \)) transported downslope [e.g. Anderson, 2002]. The evolution of \( h \) through time can be described by,

\[ \frac{dh}{dt} = \frac{p_b}{\rho_r} W + \frac{1}{\rho_r} \frac{dq_s}{dx} - p_d h \]
The first right hand term is a source associated with production of regolith from the underlying bedrock. We use a simple regolith production function based on an exponential decay (length scale \( L_0 \)) of production with regolith thickness (\( h \)) and a maximum production \( E_0 \) for exposed bedrock,

\[
\dot{W} = \frac{E_0}{\cos \theta} \exp\left(-\frac{h \cos \theta}{L_0}\right)
\]

The local slope is \( \theta \), and the \( \cos \theta \) maps vertical thickness into slope normal thickness. This formulation is based on extensive work in silicate-rich soil-mantled landscapes [Heimsath et al., 1997, 2000], but we are aware that other formulations have been proposed [e.g. Small et al., 1999; Anderson, 2002; Carretier et al., 2014].

The second right hand term represents the regolith flux \( q_s \) that evolves non linearly with topographic gradient \( \nabla z \) [Roering et al., 1999, 2007; Roering, 2008], and is linearly dependent on regolith thickness [Pelletier et al., 2013],

\[
q_s = -\frac{K_T h \cos \theta \nabla z}{1 - \left(\frac{\nabla z}{S_c}\right)^2}
\]

\( K_T \) is a transport coefficient \([L/T]\) and \( S_c \) \([L/L]\) a critical slope gradient at which regolith flux goes to infinity.

Finally, we parametrize regolith dissolution during its downslope transport as a first-order kinetic process characterized by a constant rate \( p_d \) of mass loss per units of mass and time.

## 4 Data and results

### 4.1 Denudation rate measurements with \(^{36}\text{Cl}\)

Denudation rates were calculated from \(^{36}\text{Cl}\) concentrations, based on spatial scaling factors from Stone [2000] and using the approach and parameters of the procedure proposed by Schimmelpfennig et al. [2009] which relied on the Heisinger et al. [2002] muon schemes. The natural Cl concentration of all samples is lower than 10 ppm and mostly between 4 and 2 ppm, the main production pathway for \(^{36}\text{Cl}\) is thus through Ca spallation. All analytical results are provided in table 1.

Two process blanks were treated and measured along with our samples. They contained \(0.123 \times 10^6\) and \(0.068 \times 10^6\) atoms of \(^{36}\text{Cl}\) which is two orders of magnitude lower than the \(31.2 \pm 5.6 \times 10^6\) average value in our samples. They contained \(0.052 \times 10^{18}\) and \(0.095 \times 10^{18}\) atoms of natural chlorine which is at least one order of magnitude lower than the \(3.11 \pm 1.59 \times 10^{18}\) average value.
in our samples. Measured concentrations range from 0.6 to 1.4 \(10^6\) at/g, which corresponds to denudation rates in the 30-70 mm/ka range and integrated time periods of 20 to 9 ka, respectively. The $^{36}$Cl concentrations and their corresponding denudation rates are similar within 1\(\sigma\) uncertainty for the bedrock and clasts samples, except at site 11 where the discrepancy is of about 10\% (figure 3). We note variations in the Ca content of our samples of 30-40\%, with one sample as low as 21\%, which denote a significant dolomitic component at some sites (table 1). However, such variability in the rock composition does not seem to affect the observed denudation rates.

4.2 Evolution of Hilltop curvature with denudation rates

Curvatures values measured at our sites range from $\sim0$ m$^{-1}$ at sites 6 and 12 to $\sim0.05$ m$^{-1}$ at site 4. Denudation rates progressively increase with hilltop curvature (figure 5). Starting from 30-40 mm/ka, a nearly linear trend is observed between curvature and denudation rate, consistent with transport-limited diffusive hillslope evolution. Such downslope displacement of the regolith is likely accomplished by bioturbation associated with root development [Hoffman and Anderson, 2014] and freeze-thaw cycles. For hillslope curvature larger than $\sim0.02$ m$^{-1}$ denudation rates do not increase substantially above $\sim70$ mm/ka, despite a two-fold increase in curvature. This plateau results from a behavioral change of the hillslope in which the rate of regolith production from the bedrock reaches its maximum value and cannot further increase, while curvature continues to evolve because of the ongoing hillslope relief development associated with progressive dissection and incision at the gully bottoms [e.g. Hurst et al., 2013a].

4.3 Modelling results

We define our reference model with a set of parameters that allows to reproduce the main characteristics of our dataset. We model the evolution of a 50 m long hillslope and impose, as a boundary condition, the lowering of the base level at a constant rate (100 mm/ka) at the bottom of the hillslope, which corresponds to a progressive and continuous incision of the channels. We use a transport coefficient of 0.05 m/yr, which is not dimensionally equivalent to a diffusivity coefficient due to the linear dependence on regolith thickness of the transport law presented at equation 5 [Roering, 2008; Pelletier et al., 2013]. The critical hillslope gradient $S_c$ is 0.8 and the bedrock-to-regolith density ratio of 1.5. The regolith production function (equation 4) is parametrized using a standard decrease length scale $L_0$ of 0.5 m and a
maximum rate of surface lowering $E_0$ of 80 mm/ka. For an horizontal stable surface equation 3 is simply,

$$\frac{\rho_b}{\rho_r} E_0 \exp\left(-\frac{h}{L_0}\right) = p_d h$$

(6)

This equation has no analytical solution, but can be numerically solved. Using a regolith dissolution rate of 0.01% per year produces a surface lowering of $\sim$30 mm/ka, close to observed values in the Luberon summit surface and elsewhere in peri-Mediterranean regions [Furlani et al., 2009; Ryb et al., 2014b,a].

The model displays a rapid increase of denudation at low curvature and then a slower evolution when reaching denudation rates of 60-80 mm/ka (figure 6A), which is close to the maximum regolith production $E_0$ and represents a transition toward a situation where the evolution of the system is limited by the capacity of the hillslope to produce regolith. The associated topographic evolution (figure 6B) shows a progressive increase of relief with the development of hilltop curvature, while the base of the hillslope is continuously lowered.

The use of lower or higher transport coefficients results in less or more rapid increase of denudation with curvature during the early stage of the hillslope evolution, respectively (figure 6A). The differences in rates of change in denudation become narrower at latter stages when threshold processes are dominating the regolith transport. Variations in regolith dissolution rates are mostly influencing the rate of denudation of the initial flat surface, from almost no lowering for very low dissolution rate to rates up to 60 mm/ka at dissolution equivalent to 4 times the reference value (figure 6C). Finally, variations in the characteristic length controlling the dependence of the regolith production on depth (equation 4, figure 6D) are shifting the response curve toward slower or faster evolution for lower or higher values, respectively.

Again, we strongly argue against any over-interpretation of these modelling results, as we acknowledge that some model components such as the regolith production rule are still largely unconstrained in carbonate landscapes. Our approach is mainly heuristic and a thought experiment aimed at providing a general framework for the analysis of the behaviour of such hillslope. A systematic investigation of the values of specific parameters, beyond the simple sensitivity tests presented on figure 6, is clearly not the objective of this model.
5 Discussion

5.1 Interpretation of denudation rates and controlling factors

Our rates are within the range of denudation rate values reported in global compilations [Ryb et al., 2014a]. Over flat to low-convexity surfaces, the lower bound of 30 mm/ka is slightly higher than other estimates on carbonate plateaus under Mediterranean climate [e.g. Furlani et al., 2009; Sadier et al., 2012]. The fact that $^{36}$Cl concentrations (and hence denudation rates) are comparable for bedrock and amalgamated clasts sampled at identical locations has important implications for the evolution of the regolith cover of these ridges over the time period integrated by the method. We argue that this suggests the clasts are not remnants of a thicker soil or regolith that would have been recently eroded away due to a change in climate or land use, which would have produced lower concentrations in the buried and recently exhumed bedrock than the clasts. We therefore make the assumption that the present observed conditions can be extrapolated over at least the last 9 ka, which is the lowest reported integrated time period at our sites.

We could also consider an alternative possibility, where the clasts were previously located close to the interface between the bedrock and a thicker soil layer, that was eroded at some point during the Holocene [e.g. Fuchs, 2007]. Several lines of evidence are inconsistent with this hypothesis. First, our sites are located along hillcrests, with some of them presenting a high curvature (figure 2A) where the presence of thick soil is unlikely [e.g. Heimsath et al., 1997]. Second, such rapid transfer of soil from the hillslopes to the adjacent channels is likely to exceed the local transport capacity but we did not observe significant accumulation in the valley bottoms and hollows of the northern flank of the Petit Luberon. Finally, even if the clasts had been located at the bottom of a previous thicker soil cover, they would still be stratigraphically above the bedrock surface and vertically spread over a few tens of centimeters. The well constrained exponential decrease of spallogenic production of $^{36}$Cl with depth would unambiguously lead to significantly lower $^{36}$Cl concentrations in the bedrock and a corresponding systematic deviation below the 1:1 line in figure 3, which is not what we observe.

The limiting factors on carbonate dissolution have already been thoroughly investigated by Ryb et al. [2014b,a, 2015] across the Mediterranean and arid landscapes of Israel. Mean annual precipitation is 700 mm/yr over the Luberon Mountains, where water availability is likely to be limiting chemical weathering processes [Ryb et al., 2014a]. This suggests that physical weathering develops in part because carbonate dissolution alone does not effectively
limit relief development. We observe that both physical and chemical processes operate at our sites, in particular that dissolution develops small-scale karstic networks into the rock mass that then allow release of individual clasts (figures 2 and 7). We hypothesize that the maximum observed denudation corresponds to a limit in the capacity of the hillslope to dissolve the carbonate substrata and to produce regolith from bedrock. The coupling of physical and chemical processes does not allow us to unambiguously associate this limit to one type of weathering or another. This maximum value of $\sim 70$ mm/ka is relative to the specific climatic and lithological conditions at our sites, and for example, higher precipitation would probably increase this limit. In terms of hillslope-scale evolution, this behavioral change corresponds to a transition from a transport-limited to a weathering-limited regime. While we have not carried a quantitative investigation of this parameter, it appears that bedrock exposures are significantly more widespread at the high curvature sites 1 and 4, when compared with other surveyed locations.

5.2 Regolith production and transport processes

The hillslope evolution model generally reproduces the first-order evolution of curvature and denudation observed at the field sites, and in particular the two-stages evolution, with a near-stabilization of denudation at high curvature (figure 6). In the model, the presence of this limit is a direct consequence of the existence of maximum regolith production $E_0$ in equation 4. We postulate that the evolution observed in our cosmogenic and topographic observations is the manifestation of underlying processes presenting a similar behaviour with respect to the evolution of the hillslope and regolith layer. While the actual nature of these processes is debated, it can be proposed that they are characterised by a limit corresponding to the maximum rate at which they can operate to lower the bedrock and produce regolith elements. Field observations in another carbonate massif in Western Provence (Nerthe range, figure 1A) provide some clues on the evolution of the shallow bedrock level (figure 7). We observe a transition in the degree of fracturing of the bedrock over the first meter below the surface. The uppermost part of the section displays a high fracture density which corresponds to the production of individual clasts in the 1-10 cm size range, that will be the main constituents of the regolith. Deeper in the section (20-30 cm below the surface) the spacing between fractures increases, and the bedrock appears to have been through a lesser degree of mechanical weathering. Closer views confirm that chemical and mechanical processes are jointly operating to produce the clasts, as the fracture edges are significantly smoothed by dissolution (figure 7B-C). These observations suggest that the processes that drive the fractur-
The limestone clasts produced by chemical and mechanical bedrock weathering are incorporated into the mobile regolith layer and then progressively transported downslope. Using the 0.01%/yr dissolution factor proposed above yields a characteristic time for the dissolution of 50% of clast mass of \( \tau \simeq 7 \) ka. Such survival over the 10 ka time-scale suggests that individual clasts produced at the hilltop are effectively moved away and transferred to the adjacent slopes over their life time.

5.3 Implications for relief evolution in carbonate landscapes

Our results have important implications for landscape evolution in carbonate-dominated settings, as they illustrate an abrupt limit of weathering processes to produce clasts and to lower the hillslope at a pace that matches the local...
base level fall. Such limitation of weathering below $\sim 70$ mm/ka may prevent the hillslope/channel system from reaching an equilibrium shape and lead to an increase in hillslope relief. We observe such transient evolution in our study area where the lower parts of the range display near-threshold hillslope angles and high local relief, whereas the low-relief summit area is dominated by continuous slope-dependent hillslope evolution processes (figure 8). At a global scale we note that Mediterranean landscapes often display high local relief at 1-10 km wavelengths, with common occurrence of prominent limestone cliffs up to several hundred meters high. Our observations in the Luberon Mountains suggest that such relief could be a consequence of the inability of local weathering processes operating at the hillslope scale to keep pace with the dissection of topography by the fluvial network.

Ryb et al. [2013] report a significant change in landscape dynamics in the Judea Hills of Israel occurring around the mid-Pleistocene, from a situation where active landsliding was the dominant denudation process, toward hillslopes controlled by largely slope-independent dissolution. They interpret the present-day landscape as mostly inactive in terms of mechanical and gravity driven processes with long-wavelength features mostly inherited from the previous stage. The landscape of the northern flank of the Luberon mountain is in a transient state and dynamically adjusting during its evolution and we do not observe characteristics features of remnant topography such as large knickpoints or massive alluvial and colluvial deposits. The contrast between the near threshold hillslopes and cliffs of the lower part of the range and our studied area near the summit surface (figure 8) is a manifestation of the transition from a landscape dominated by diffusion dominated processes, toward a regime where hillslope failure and rapid mass movement assume a larger role in landscape evolution (figure 1C). We consider both parts to be active, and to represent two distinct stages in a progressive transient evolution of the range.

6 Conclusions

We have documented denudation across a carbonate range of South-Eastern France. Flat surfaces that are unaffected by gravity driven processes lower at 30-40 mm/ka, which is consistent with other observations on similar surfaces in peri-Mediterranean regions. While investigations of the relationship between hillslope convexity and denudation are almost as old as Geomorphology [Gilbert, 1909] and central to many hillslope evolution models, there is currently only a limited number of studies which document their co-evolution, and in particular the linear relationship we observe on figure 5.
For our highest curvature sites we observe that denudation reaches a plateau at $\sim 60$-$70$ mm/ka, which we interpret as a transition from transport-limited to weathering-limited evolution. Such change in behavior may promote the development of high local relief in Mediterranean landscapes as hillslopes become unable to match the imposed pace of base level lowering. Further investigations will attempt to address the dependence of the pattern we observe on figure 5 to different climatic settings in terms of precipitation and temperature.

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Table 1: Analytical results for the samples processed in this study
Figure 1: A - General situation map of the studied region (Provence, southeastern France), with the location of the main carbonate ranges. B - Situation map of the Petit Luberon mountain (IGN BDALTI DEM). C - Orthophotography of the main sampling area (IGN BDORTHO database), and main geomorphological features based on field surveys and air photos analysis. Samples are color coded according to their denudation rate. Thin white contour lines separation is 20 m. Site 12 was sampled farther east, where the summit surface is the widest.
Figure 2: Field photographs illustrating geomorphological features of the Petit Luberon northern flank. A-B - Views along the ridge axis looking toward the north for sites 1 and 11, respectively. C - In-situ frost or bioturbation assisted fracturing contributing to the separation of individual clasts from the bedrock, observed at site 10. D - Pre-existing fractures and structural bedding contributing to the separation of individual clasts from the bedrock, observed at site 8. E - View of clasts pavements at the surface of site 2. F - Weathered and rounded clasts at the surface of site 8, showing a clear distinction between the lower part of the clast embedded in the regolith (white, rounded and polished surface) and the upper part directly exposed at the surface (greyish surface partly covered with lichens).
Figure 3: Comparison of $^{36}$Cl concentrations in bedrock and amalgamated clasts samples at a same location.

Figure 4: A - Aerial view of sampling site 8 (figure 1C), with sampling location and radius of calculation (15 m) for the curvature. B - Evolution of calculated curvature at site 8 with the radius of the calculation area. Light blue envelope indicates the $\pm 1\sigma$ interval. Dark vertical line indicates the reference radius used in this study. C - Cross ridge topographic profile at site 8 (light gray points). Dark gray background indicates the calculation area for curvature corresponding to a 15 m radius around the sampling site. Solid thick red curve is quadratic fit through the data points.
Figure 5: Denudation rates against hilltop curvature measured at our sampling sites. Large dark blue circles represent denudation rates measured from amalgamated clasts samples, whereas small light blue circles represent bedrock samples. The dark gray background curve is a prediction from a 1D diffusive hillslope evolution model (figure 6). The light gray line and envelope (95% confidence) are a linear fit through the data for curvature <0.02 m$^{-1}$. 
Figure 6: Modelling results. In all insets A, C and D the thick line is the reference model. Grey circles in the background are the data points for the several sites presented in this study (figure 5). A - Test of the influence of 2-fold variations for the transport coefficient $K_T$ (reference value 0.05 m/yr). Dots along the curves are indicating 100 kyr time intervals since the initiation of channel incision at the base of the hillslope. B - Hillslope topography evolution (top) and regolith thickness (bottom) at the time intervals indicated on inset A (constant lowering rate of 100 mm/kyr). All topographic profiles have their hilltops aligned as a reference (hilltop surface are actually progressively lowered with respect to their initial position by dissolution). C - Test of the influence of 4-fold variations of the regolith dissolution rate (reference value 0.01 %/yr). D - Test of the influence of 2-fold variations of the e-folding decay length-scale of the regolith production function $L_0$ (reference value 0.5 m).
Figure 7: Field photographs of a bedrock section in the Nerthe massif (west of Marseille, N43.3437-E5.2397). See figure 1A for location. A - General view of the section showing the difference in bedrock fracturing with depth. B-C - Closer view illustrating the smoothing action of carbonate dissolution on fracture edges.

Figure 8: A - Topographic gradient map over the main sampling area. Vertical bars indicate the width of the swath profile presented on inset B. White circles are sampling sites (figure 1C). B - North-south profile across the northern flank of the Petit Luberon. Red solid and dashed lines are the mean and extreme values of elevation. Intensity of blue background indicates the frequency distribution of hillslope gradients.