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Effective ion mobility in anion exchange ionomers: relations with hydration, porosity, tortuosity, and percolation

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ABSTRACT

The effective mobility of hydroxide, chloride and fluoride ions is reported in various anion exchange membranes (AEM) with a backbone of polysulfone (PSU) or poly(2,6-dimethyl-1,4-phenylene)oxide (PPO). The concentration dependence of the effective mobility is used to derive the porosity (π), tortuosity (τ), and percolation thresholds and to plot the ionic conductivity *vs* the hydration number. Semi-logarithmic plots of the effective ion mobility $u(i)$ *vs* the square root of concentration $\sqrt{c(i)}$ for hydroxide, fluoride and chloride ions in various PSU- and PPO-based ionomers at 25 and 60 °C show linear relations, from which the ratio π/τ can be determined. This existence of linear $u(i)=f(\sqrt{c(i)})$ plots is related to the very particular boundary conditions experienced by mobile ions, migrating in close vicinity to the immobile grafted counter-ions placed at the interfaces between polymer domains and electrolyte solution. The π/τ values for PSU-QA (0.29) and PPO-QA (0.38) are consistent with a relatively low hydrophilic-hydrophobic nanophase separation, which leads to channels with low diameter and high tortuosity. The tortuosity determined from a Bruggeman-type relation is 1.9 for PSU-QA and 1.6 for PPO-QA. The percolation thresholds $\phi_{H_2O,p}$, determined from the universal percolation equation near and above $\phi_{H_2O,p}$, are at a water volume fraction of 0.07 for PSU-TMA and 0.03 for PPO-QA indicating that these AEM have a two-dimensional structure of the hydrated domains. The prefactor, which should represent a good indication as to the maximum achievable ionic conductivity, is slightly below 100 mS/cm for both PSU-TMA and PPO-based ionomers. Plots of experimental and computed hydroxide and chloride ion conductivities as function of the hydration number (λ) show a maximum ionic conductivity for a value of the hydration number around 60, corresponding to optimal hydration conditions. At $\lambda = 100$, the ratio of conductivity between PSU-QA (OH^- form) and PPO-QA (Cl^- form) indicates that the degree of dissociation of ion pairs is about 30% lower for hydroxide than for chloride ions, which is consistent with the effective ionic radii of Cl^- and OH^- .

1. Introduction

The ionic conductivity of ion exchange membranes is a critical property for their application as separators in various electrochemical energy technologies, such as fuel cells, electrolyzers, or redox flow batteries [1-4]. A low ion conductivity increases the area specific resistance of the devices and the Ohmic drop of the electrochemical cell and reduces the energy conversion efficiency by heat production [5, 6].

Generally, the ionic conductivity is the sum of the partial conductivities of various ions that depend on three factors: the charge of the ion (equal to the Faraday constant F for molar quantities and a singly charged ion), the ion concentration and the ion mobility. The case of ion exchange polymers is peculiar, because only one type of ion is mobile in the internal electrolytic solution, whereas the counterions are grafted on the polymer backbone and immobile [7-9]. The ion concentration can be modified by a change of the ion exchange capacity (IEC) of the ionomer and/or a change of its hydration [10-12].

The mobility of a single monovalent ion $u(i)$ is defined according to equation 1 by the ionic conductivity $\sigma(i)$ (expressed in mS/cm) and the ion concentration $c(i)$ (expressed in mol/L):

$$u(i) = \frac{\sigma(i)}{F \cdot c(i)} \quad (1)$$

The ion mobility is a complex parameter in an ionomer, given that it reflects the conditions of ionic motion in the restricted area of nanometric ion conduction channels present in the hydrated ionomers, but also the particular electrostatic conditions, where the mobile ions migrate inside channels with immobile counterions grafted on the channel walls [13-15]. This situation reduces the ion mobility by electrostatic interactions. Furthermore, the ionic transport depends on the percolation of the hydrated channels and their tortuosity [16, 17]. The percolation threshold is reached when the hydrated clusters become interconnected and long-range ionic conduction is possible [18]. The cross-section available for ionic conduction is proportional to the effective size of the hydrated channels; it is only a fraction of the total cross-sectional area of the ionomer, expressed phenomenologically by the “porosity” π ($0 < \pi < 1$) [19-21]. Moreover, not all pores have the same transport efficiency: the “tortuosity” τ is also a phenomenological parameter, which describes the complex interconnected pore network with irregular shapes and cross sections ($\tau > 1$) [17]. $1/\tau$ is the fraction of pore volume having the same efficiency for transport as the bulk electrolyte [16]. The percolation threshold, porosity and tortuosity are a function of the nanophase separation, which is

associated to the hydrophilicity of the ionic groups and the hydrophobicity of the polymer backbone [22]. Phase-separated morphologies are also related to the temperature and the solvent-polymer and polymer-polymer interactions, described by the Flory-Huggins theory [23].

Various authors have investigated the effective ion mobility dependence on the ion concentration for proton-conducting ionomers [10, 11, 22, 24-29]. We have previously reported the proton mobility dependence on concentration in various sulfonated aromatic polymers (SAP) and perfluorinated sulfonic acid (PFSA) polymers [30-33] and deduced percolation thresholds and tortuosity values [30, 31, 34].

For anion exchange membranes (AEM), the groups of Kreuer [35], Dekel [36], Benziger [37] and Hickner [36, 38] reported anion conductivity data and discussed their relevance. Paddison and coworkers published mesoscale simulations of AEM [39]. Wu et al. discussed the hydroxide ion mobility in poly(ether ether ketone) based AEM [37, 40]. In the case of AEM, the dissociation of ion pairs [41] is incomplete, reminiscent of the so-called “Manning condensation” in polyelectrolytes [42].

In this paper, we report the effective mobility of hydroxide, chloride and fluoride ions in various ionomers with a backbone of polysulfone (PSU) or poly(2,6-dimethyl-1,4-phenylene)oxide (PPO) and quaternary ammonium (QA) groups. The concentration dependence of the effective mobility is applied to derive the tortuosity and percolation parameters and to establish the relation between conductivity and hydration number. The relevance of these data for practical applications of AEM as ion-conducting separators in electrochemical devices is also discussed.

2. Experimental

2.1. Products

PSU (MW = 55500 g/mol) was purchased from Solvay. PPO (MW = 50000 g/mol), 1,5,7-triazabicyclo[4.4.0]dec-5-ene (TBD) trimethylamine (TMA, 4.2 M in ethanol), 1,4-diazabicyclo[2.2.2]octane (DABCO), paraformaldehyde ((CH₂O)_n), trimethylchlorosilane (Me₃SiCl), SnCl₄, 1,4-dibromobutane, dimethylsulfoxide (DMSO), and N-methyl-2-pyrrolidone (NMP) and all other chemicals were reagent-grade and purchased from Sigma-Aldrich.

2.2. Ionomer synthesis

The synthesis of the various ionomers was described in the following references: PSU-TMA and PSU-DABCO [43], PPO-DABCO with long side chain [44]. In short, PSU-TMA and PSU-DABCO were prepared by the chloromethylation route. Different degrees of chloromethylation were obtained varying the reaction time. Chloromethylated PSU samples (PSU-CH₂Cl) reacted with TMA and DABCO via nucleophilic substitution (quaternization). PPO-DABCO with long side-chain was prepared by benzyl bromination followed by quaternization. Cross-linked AEM (XL-AEM) were synthesized using 5% of chlorosulfonated poly(ether ether ketone) (PEEK-SO₂Cl) as cross-linker [43].

PPO-DABCO was prepared by the chloromethylation route using the following ratio of reagents PPO:Me₃SiCl:(CH₂O)_n:SnCl₄ = 1:3:3:0.05. Before the use, chloroform was washed with water to remove ethanol and dried on molecular sieves (3 Å). All the steps were carried out under nitrogen in anhydrous conditions. PPO (41.8 meq) was dissolved in 250 mL of CHCl₃ at RT, then the temperature was increased to 45 °C. At the same time Me₃SiCl, paraformaldehyde, and SnCl₄ were mixed and heated to 45 °C. After 1 h, a clear solution was obtained. This solution was quickly added to the solution of PPO and the reaction performed at 45 °C for a time in the range 8-17 h in order to obtain different degrees of chloromethylation. After this time, the temperature was reduced to RT and 150 mL of CH₃OH added until complete precipitation. The PPO-CH₂Cl was washed with CH₃OH and dried in the oven at 60 °C for 48 h [45].

The quaternization was carried out in NMP for 72 h at 70 °C with a ratio between functional groups of PPO-CH₂Cl and DABCO 1:1.4. After this time, the solution was reduced to a third under low pressure at 80 °C and directly used for the casting procedure. The ion exchange capacity (see Table 1) was measured by Mohr titration [44].

2.3. Composite AEM

The ionomer composites (see Table 1) were prepared using TiO₂ functionalized with poly(methylhydrosiloxane) [46] or layered double hydroxides (LDH) as fillers. The synthesis of Mg/Al LDH was described in reference [47].

2.4. Membrane preparation

The membranes were generally prepared by dissolution of the ionomers in NMP, typically 250 mg per 20 mL of solvent, and casting at 100 °C before drying in an oven at 90-100 °C during 48 h.

For composite AEM, the nanometric inorganic filler was added to the ionomer solution before casting (between 5 and 30 wt%) and sometimes DMSO was preferred to NMP to assure a better homogeneity of the samples. The detailed procedures for composites can be found in the following references: PSU-DABCO-TiO₂ [46], PSU-TMA-LDH [47] and PSU-DABCO-LDH [47, 48]. PPO-DABCO-LDH was obtained by adding 30 wt% of LDH to 20 mL of a 0.05 M solution of PPO-DABCO in NMP. The mixture was evaporated to a half of the initial volume during vigorous stirring and the viscous solution was cast onto a Petri dish and heated in an oven at 100 °C during 48 h.

2.5. Determination of the IEC

The IEC (meq/g) is expressed in milliequivalents of ionic groups n per mass of dry polymer m_{dry} :

$$IEC = \frac{n}{m_{dry}} \quad (2)$$

The ion exchange capacity was determined by acid-base titration or by Mohr titration. For the latter, the ionomer was first ion-exchanged in a 1 M NaCl solution during 24 h and carefully washed in deionized water during 24 h. The polymer dried in a desiccator during 48 h was immersed in Na₂SO₄ solution and the exchanged Cl⁻ ions were titrated with 0.1 M AgNO₃ solution. 1 mL of 0.25 M K₂CrO₄ indicator solution was added prior to the titration. At the equivalence point, a red-brown precipitate of Ag₂CrO₄ appeared.

2.6. Water uptake measurements

The water uptake (WU) is determined from the masses of dry and wet polymer (m_{wet}); it is related to the volumes of water and dry polymer via the dry polymer density ρ_{dry} :

$$WU = \frac{m_{wet} - m_{dry}}{m_{dry}} = \frac{m_{H_2O} + m_{dry} - m_{dry}}{m_{dry}} = \frac{m_{H_2O}}{m_{dry}} = \frac{V_{H_2O}}{V_{dry}\rho_{dry}} \quad (3)$$

The densities of the electrolytic solutions are approximated as 1 g/cm³. Experimental values determined in Nafion are near 1 and the concentration dependence of the electrolyte density is small [49]. We assume that all water molecules reside near ionic groups for thermodynamic affinity reasons (in agreement with the definition of the hydration number) and that the concentration of the internal electrolytic solution is homogeneous throughout the membrane. Combining equations 2 and 3, one obtains:

$$WU = \frac{V_{H_2O} \cdot IEC}{n} \quad (4)$$

The hydration number, which is the number of water molecules per ionic group, is defined as:

$$\lambda = \frac{1000 \cdot WU}{IEC \cdot M(H_2O)} \quad (5)$$

$M(H_2O)$ is the molar mass of water.

The measurements were made on ionomers in hydroxide, chloride or fluoride forms. The samples were obtained by ion exchange in 1 M solutions of NaOH (under nitrogen), NaCl or NH_4F during 24 h. After the ion exchange, the samples were carefully washed in deionized and decarbonated water during 24 h to remove any excess of electrolyte. The hydroxide forms were analyzed immediately or stored in absence of CO_2 to avoid carbonation issues. The mass of wet samples (m_{wet}) was determined after immersion during 24 h in deionized water and wiping the sample surface with absorbing paper. The mass of dry samples (m_{dry}) was measured after storing them over P_2O_5 in a desiccator during 48 h.

2.7. Ion conductivity measurements

AEM samples in hydroxide, chloride, or fluoride forms were made as described above. The fully humidified membranes were immediately placed in Swagelok holders with stainless steel electrodes (*through-plane* configuration). Electrochemical impedance spectroscopy measurements were performed using a Biologic VSP-300 apparatus. The applied a.c. voltage was 20 mV and the frequency range 1 Hz-6 MHz. The impedance spectra were interpreted by non-linear least-square fitting using a classical Randles circuit (R_1 - R_2 //CPE) or a series of two parallel circuits containing a resistance and a constant phase element (R_1 //CPE $_1$ - R_2 //CPE $_2$). The ionic conductivity at partial humidification ($65 \leq RH / \% \leq 95$) was measured with *in-plane* configuration using the apparatus described in reference [47].

3. Results

The chemical formulas of PSU-TMA, PSU-DABCO, PPO-DABCO, and PPO-DABCO with long side-chain are shown in Figure 1.

Table 1 presents the experimental results for IEC, WU and ionic conductivity for the various investigated AEM.

Table 2 shows the IEC, WU and ionic conductivity data of PSU-TMA and PSU-DABCO as well as composites with LDH at 60 °C and 95, 80 or 65% RH.

The values of WU (in %) must be divided by 100 in all equations.

Figure 1. Chemical formulas of a) PSU-TMA, b) PSU-DABCO, c) PPO-DABCO, and d) PPO-DABCO with long side-chain.

Table 1. Ion exchange capacity (IEC), water uptake (WU), and ionic conductivity (σ) of various PSU and PPO-based ionomers at 25 °C.

Samples	IEC (meq/g)	WU (%)	σ (mS/cm)	Samples	IEC (meq/g)	WU (%)	σ (mS/cm)
PSU-based AEM (OH⁻ form)				PPO-based AEM (Cl⁻ form)			
DABCO [43]	1.10	33.0	5.3	DABCO	0.88	15.7	0.5
DABCO [46]	1.25	85.0	5.1	DABCO	0.91	22.1	0.9
DABCO [47]	1.57	124.3	5.3	DABCO	1.10	22.8	1.1
DABCO [43]	1.70	504.0	6.7	DABCO	1.48	30.4	1.2
DABCO-TiO ₂ [46]	1.25	56.0	4.3	DABCO	1.60	30.6	2.0
DABCO-LDH [47]	1.57	25.4	2.2	DABCO long chain [44]	1.30	21.0	1.4
TMA [43]	0.81	19.0	2.2	DABCO-LDH	0.91	39.5	0.9
TMA 5% XL* [43]	0.81	26.0	2.3	DABCO-LDH	1.67	36.4	1.0
TMA 5% XL** [43]	1.19	32.0	2.2	DABCO-LDH	1.69	39.8	1.3
TMA 5% XL*** [43]	1.19	319.0	4.3	PSU-based AEM (F⁻ form)			
TMA [43]	1.34	40.0	4.6	DABCO (F ⁻ form) [50]	1.30	198.0	5.8
TMA [43]	1.64	53.0	12.0	TMA (F ⁻ form) [50]	1.64	130.0	9.5
TMA-LDH [47]	1.67	42.1	3.7				

* Cross-linked (XL) ionomer

** XL ionomer annealed 24 h at 120 °C

*** Strongly hydrated XL ionomer

Table 2. Ion exchange capacity (IEC), water uptake (WU), and hydroxide ion conductivity (σ) of PSU-based ionomers at 60 °C and various relative humidity values (RH) [47].

Samples	IEC (meq/g)	RH (%)	WU (%)	σ (mS/cm)
TMA	1.67	95	40.0	81.0
		80	36.1	49.6
		65	33.1	28.0
TMA-LDH	1.67	95	26.2	26.6
		80	22.8	14.7
		65	17.7	7.4
DABCO	1.57	95	34.8	45.7
		80	29.1	23.0
		65	25.7	8.9
DABCO-LDH	1.57	95	28.0	30.0
		80	25.1	17.9
		65	19.8	5.5

4. Discussion

The ion concentration in the electrolytic solution inside the ionomer channels, expressed in mol/L, can be calculated from *IEC* and *WU* (combining eq. 2-4). $c(i)$ is directly related to the hydration number λ (cf. eq. 5):

$$c(i) = \frac{IEC}{WU} = \frac{1000}{\lambda \cdot M(H_2O)} \quad (6)$$

Changes of the ion concentration due to an incomplete dissociation or the formation of ion pairs are observed in the effective ion mobility defined by eq. 1.

Figure 2 shows a semi-logarithmic plot of the effective ion mobility at 25 °C vs the square root of concentration for hydroxide and fluoride ions in PSU-TMA and PSU-DABCO ionomers (triangles) as well as chloride ions in PPO-DABCO based ionomers (dots). Figure 3 shows a comparison of hydroxide ion mobilities in PSU-QA ionomers at 25 and 60 °C with literature data for proton-conducting SPEEK [31]. We present the data for PSU-DABCO and PSU-TMA with identical symbols in Fig. 3, because there is no significant difference between the two data sets, confirming that the nature of the amine is less important for the anion mobility, as already stated [43].

One should mention that the hydroxide ion mobilities at 60 °C (calculated from the data in Table 2) were obtained by in-plane measurements [47, 51, 52], which give somewhat higher ionic conductivities, due to a surface segregation of functional groups [51]. Literature values for the activation energy of hydroxide ion migration are between 0.1-0.2 eV [53-56], but above 0.2 eV for $\lambda < 20$ [35].

This $u(i)$ vs. $c(i)^{1/2}$ plot type is selected following the classical square root concentration dependence of the equivalent conductivity of electrolyte solutions (“Kohlrausch law” [57-59]). A linear decrease with the square root of concentration is observed for strong electrolytes. In “weak” electrolytes, the concentration dependence of the equivalent conductivity is much stronger, due to the incomplete dissociation, which becomes complete only at infinite dilution [36, 58]. Polyelectrolyte solutions also do not obey the linear limiting law, which is attributed to the high charge density of the polyions and to the flexibility of the polyion chain and its ability to change conformation [60]. A similar strong concentration dependence is here observed for the electrolyte solutions inside ionomers, including those containing strong sulfonic acids, such as SPEEK (Figure 2) and Nafion [30, 34]. The very

particular boundary conditions experienced by the mobile ions, migrating in close vicinity to the fixed opposite charges of the grafted ionic groups placed at the interfaces between polymer domains and electrolyte solution, leads to a strong concentration dependence of the effective ion mobility. It reflects the concentration-dependent formation of ion pairs or complexes of several ions that break apart only at high water content [35].

Figure 2. Concentration dependence of the effective mobility of hydroxide and fluoride anions in PSU-based ionomers and chloride anions in PPO-based ionomers with quaternary ammonium groups.

Figure 3. Square root concentration dependence of the effective mobility of hydroxide anions in PSU-based ionomers with quaternary ammonium groups at 25 and 60 °C and a comparison with the proton mobility in SPEEK from reference [31].

4.1. Porosity and tortuosity

The ratio of porosity and tortuosity can be determined from the renormalisation equation 7 [17, 31, 34, 61], where $u(i)^\circ$ is the ion mobility at infinite dilution in an aqueous solution not contained in the ionomer matrix.

$$u(i) = \frac{\pi}{\tau} \cdot u(i)^\circ \quad (7)$$

The proton, hydroxide and chloride ion mobility data at 25 °C are used to extrapolate the ion mobility at infinite dilution, which can be compared with reference literature data. Consistent values for H^+ ($36.2 \cdot 10^{-4} \text{ cm}^2 \text{ s}^{-1} \text{ V}^{-1}$), OH^- ($20.5 \cdot 10^{-4} \text{ cm}^2 \text{ s}^{-1} \text{ V}^{-1}$), and Cl^- ($7.9 \cdot 10^{-4} \text{ cm}^2 \text{ s}^{-1} \text{ V}^{-1}$) can be taken from various references [57, 58, 62, 63]. Let us recall that although strong ion pairs are formed in AEM, they are totally dissociated at infinite dilution.

Equation 7 is applied to deduce the ratio porosity/tortuosity from Figure 2 for PSU-QA ($\pi/\tau = 0.29$) and PPO-QA ($\pi/\tau = 0.38$) and from Figure 3 for sulfonated poly(ether ether ketone) (SPEEK, $\pi/\tau = 0.61$). Sulfonated aromatic polymers, such as SPEEK, present a lower hydrophilic/hydrophobic nanophase separation than Nafion [22, 64, 65]; two reasons for this difference are that the sulfonic group has a lower acidity and hydrophilicity than the strongly acidic perfluorosulfonic group and that the aromatic backbone is less hydrophobic than the perfluorinated polymer backbone (it contains e.g. ether linkages). Other factors, such as chain flexibility, entanglement defects, crystallinity, and the various interaction parameters affect the nanophase separation. AEM with quaternary ammonium groups present an even lower nanophase separation, because the functional groups are less hydrophilic than sulfonic acids [35, 66]. The lower π/τ values for PSU-QA and PPO-QA are consistent with a lower hydrophilic-hydrophobic nanophase separation, which leads to channels with low diameter (low π) and high tortuosity τ (for example more dead-ends [8]). The lowest value for PSU-QA corresponds to the larger hydrophilicity of the PSU backbone vs. PPO, due *inter alia* to the presence of sulfone groups, which further reduces the nanophase separation and the porosity/tortuosity ratio, leading to narrower hydrophilic channels and to a larger separation between the functional groups [67].

Phenomenological relations exist between porosity and tortuosity; the best known is the Bruggeman-type expression [61]:

$$\tau = \pi^{-(\alpha-1)} \quad (8)$$

α is the universal percolation exponent [30, 68]. Assuming three-dimensional percolation ($\alpha \approx 2$), one obtains a tortuosity of 1.9 for PSU-QA and 1.6 for PPO-QA, in good agreement

with the values reported for PSU-QA ($\tau = 1.83-1.88$ [36]) and for a PPO-based copolymer ($\tau = 1.8$ [56]).

4.2. Percolation

The ionic conductivity can be written near and above the percolation threshold as a function of the volume fraction of the hydrated domains ϕ_{H_2O} [18, 69]:

$$\sigma(i) = \sigma(i)^\circ \cdot (\phi_{H_2O} - \phi_{H_2O,p})^\alpha \quad (9)$$

The universal percolation exponent α is near 2 for three-dimensional (3D) percolation [30, 68]. $\phi_{H_2O,p}$ is the water volume fraction at the percolation threshold and $\sigma(i)^\circ$ is the prefactor. By simple mathematical transformation of eq. 9, one can show that a plot $\sigma(i)^{1/2} = f(\phi_{H_2O})$ should give a straight line; $\sigma(i)^\circ$ and $\phi_{H_2O,p}$ can be determined from its slope and intercept, respectively.

The volume fraction of water ϕ_{H_2O} in the wet ionomer is defined and related to WU (cf. eq. 3) by eq. 10:

$$\phi_{H_2O} = \frac{V_{H_2O}}{V_{H_2O} + V_{dry}} = \frac{WU \cdot \rho_{dry}}{1 + WU \cdot \rho_{dry}} \quad (10)$$

The volume fraction ϕ_{H_2O} can be related to the IEC and the ion concentration combining eq. 6 and 10:

$$\phi_{H_2O} = \frac{IEC \cdot \rho_{dry}}{c(i) + IEC \cdot \rho_{dry}} \quad (11)$$

The dry density ρ_{dry} of the polymers is taken as 2.07 g/cm³ for Nafion [14], 1.34 g/cm³ for SPEEK [70], or by the values for PPO (1.06 g/cm³ [71]) and PSU (1.24 g/cm³ [72]). Using experimental values for each membrane might further improve the quality of the fits. Figure 4 shows such a plot for PSU-TMA and PPO-QA and a comparison with SPEEK [31] and reference data for Nafion [8].

Figure 4. Determination of the percolation threshold for AEM, SPEEK and Nafion.

The percolation threshold $\phi_{H_2O,p}$ is at a water volume fraction of 0.01 for Nafion and somewhat higher, but not that much for PSU-TMA (0.07) and PPO-DABCO ionomers (0.03), whereas it is much higher for SPEEK (0.21). Indeed, no percolation threshold is observed for PSU-QA in Figure 3, whereas it is clearly visible for SPEEK. The percolation threshold for conduction paths to traverse the ionomer, $\phi_{H_2O,p}$, is reported in SPEEK at a water volume fraction below 0.3, consistent with a stochastic medium with randomly dispersed spherical hydrated clusters [21, 61, 73, 74]. Pisani et al. fit conductivity data for SPEEK with $\phi_{H_2O,p} = 0.22$, in excellent agreement with our result [61]. Lamellar hydrophilic domains, supposed to exist in Nafion, percolate through the hydrophobic matrix at a volume fraction below 0.1 [13, 18, 73, 74], which is much lower than the value for a completely random system. Pisani et al. take $\phi_{H_2O,p} = 0$ for the simulation of Nafion conductivity data [61].

The low percolation threshold value for PSU-TMA and PPO-DABCO (well below 0.1, like that reported for PEEK-QA [37]) seems to indicate that these AEM present also a partly two-dimensional (2D) structure of the hydrated domains, but less pronounced than Nafion (“layered morphologies” [75]). Indeed, SAXS investigations suggested nanometer-range swelling to occur in two dimensions in AEM with polymer chains having a tendency to arrange locally in a parallel fashion [35]. Mesoscale simulations support this picture of layered morphology [39]. The particularly low percolation threshold for PSU-TMA is consistent with the low nanophase separation in PSU-QA (see above), which leads to narrower hydrophilic channels than in PPO-QA. It is well known that percolation thresholds

are displaced to lower volume fractions, when the domain size of the percolating phase decreases (correlation effects) [76, 77].

The prefactor $\sigma(i)^\circ$ represents mathematically the ionic conductivity when $(\phi_{H_2O} - \phi_{H_2O,p}) = 1$, corresponding to a “bulk” electrolyte experiencing similar electrostatic boundary conditions than in the ionomer. The prefactor $\sigma(i)^\circ$ depends on the particular conduction mechanism within and between two adjacent clusters, involving interactions among ions, water molecules, and the ionomer [13]. The prefactor should therefore represent a good indication as to the maximum achievable ionic conductivity in an ionomer. Indeed, $\sigma(i)^\circ$ is much higher for Nafion (~ 700 mS/cm) and SPEEK (223 mS/cm) than for PSU-TMA (86 mS/cm) and PPO-DABCO (93 mS/cm) in good accordance with the larger mobility of protons vs. hydroxide ions and the larger tortuosity of AEM.

4.3. Hydration dependence of the ionic conductivity

The presence of a solvent with high dielectric constant, especially water, is fundamental for the particular conduction mechanism in ionomers. However, hydration has antagonistic effects on the conductivity, because a large hydration increases the effective ion mobility, but reduces the ion concentration.

Figure 5 shows a plot of the proton, hydroxide and chloride ion conductivity in ionomers as function of the hydration number. The dots correspond to experimental data from Tables 1 and 2 or reference [31] for SPEEK. The lines are computed from the ion concentrations and effective ion mobilities. These plots show a maximum ionic conductivity for an intermediate value of the hydration number, corresponding to optimal hydration conditions, around 60 for AEM and 80 for SPEEK. The maximum conductivities are still significantly below the prefactors obtained from the percolation approach above, indicating that there is still substantial room for improvement of the ionic conductivity of these ionomers.

Figure 5. Experimental and computed ionic conductivity dependence on the hydration number for protons [31], hydroxide and chloride ion-conducting ionomers at 25 °C.

For large hydration numbers, the aqueous channels are fully percolating and the sulfonic acid groups are fully dissociated, but the ion pairs in AEM not necessarily, so that the ion concentration calculated according to eq. 6 is overestimated and the effective mobility calculated is underestimated according to eq. 1. At $\lambda = 100$, the ratio of conductivity for SPEEK and PPO-QA amounts to 4.6, whereas the mobility ratio at infinite dilution is 5.3 [57, 58]. Assuming that this difference is related only to the incomplete dissociation of ion pairs in PPO-QA would lead to a dissociation degree of 85% for Cl^- ions. This value is somewhat higher than the values of around 50% reported by Kreuer et al. for the Cl^- dissociation in a related AEM [35]. Laidler et al. reported a dissociation constant of 28 for tetramethylammonium iodide in acetone solution that would give similar dissociation degrees [78]. However, there are two major differences with AEM, which have an antagonistic effect on ion pair dissociation: the solvent acetone has a low dielectric constant, but the acetone solution is not contained in an ionomer with its very particular electrostatic situation.

Finally, making a similar comparison of the conductivity ratio of PSU-QA (OH^-) and PPO-QA (Cl^-), which is 1.8 at $\lambda = 100$, and the ratio of the ion mobility of hydroxide and chloride ions at infinite dilution (2.6 [57, 58]), the difference might again be attributed to the

different dissociation degree of ion pairs indicating that the degree of dissociation of ion pairs would be about 30% lower for hydroxide than for chloride ions. This result is consistent with the effective ionic radii of chloride (181 pm [79]) and hydroxide ions (132 pm [79]) given that a lower ion radius increases the strength of ion pairs [80-82].

5. Conclusions

The effective ion mobility in ionomers is a key property in order to reach ionic conductivities high enough to design ionomer separators for electrochemical devices with low area specific resistance. The effective ion mobility is a complex parameter, which depends on the complicated situation encountered by the mobile ions during their migration in the restricted area of ion conduction channels surrounded by a solvent with high dielectric constant and fixed counter-ions grafted on the channel walls. This complexity can be described by several phenomenological parameters, such as porosity and tortuosity, percolation threshold, degree of dissociation of ion pairs.

In this work, we determined and analysed the effective anion mobility in various anion exchange membranes with PSU or PPO backbones. Linear semi-logarithmic plots of the effective ion mobility vs. the square root of the ion concentration allowed determining the ratio porosity/tortuosity. The values of AEM (PSU-QA: $\pi/\tau = 0.29$ and PPO-QA: $\pi/\tau = 0.38$) are inferior to those of proton exchange membranes (SPEEK, $\pi/\tau = 0.61$). This finding can be attributed to a lower nanophase separation, due to the minor hydrophilicity of quaternary ammonium groups vs sulfonic acids. The smaller value for PSU-QA with respect to PPO-QA is related to the lower hydrophobicity of the ionomer backbone, due to the more hydrophilic sulfone moieties and the absence of methyl groups.

The percolation threshold was determined from linear plots of the square root of ionic conductivity vs. the volume fraction of aqueous domains. The low percolation threshold of AEM (PSU-TMA: $\phi_{H_2O,p} = 0.07$ and PPO-QA: $\phi_{H_2O,p} = 0.03$) indicates the existence of 2D arrangements of the ionic domains, which percolate at lower water fractions than 3D domains. This finding is in agreement with the conclusions of literature SAXS experiments.

The ion conductivity shows a maximum for a hydration number around 60 for AEM, which corresponds to an optimal compromise of anion concentration and effective anion mobility. The ratio of conductivities for chloride and hydroxide ions indicates that the degree of dissociation of ion pairs is about 30% lower for OH^- ions. This conclusion is consistent

with the lower radius of hydroxide ions, because the strength of ion pairs, due to Coulombic interactions, is related to the inter-ionic distance.

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Graphical abstract